B.Sc. DEGREE PROGRAMME

CHOICE BASED CREDIT SEMESTER SYSTEM

(CBCSS-UG Regulations 2019)

B.Sc. MATHEMATICS AND PHYSICS DUAL CORE PROGRAMME

(Language Reduced Pattern(LRP))

SYLLABUS

(Effective from 2020 admission onwards)



UNIVERSITY OF CALICUT

Syllabus structure

The following courses are compulsory for the BSc Mathematics and Physics Dual Core programme.

						M	Max. Marks				
Semester	Code	Name of the course	Total No Contact hours	No of contact hours/Week	Credits	Internal	External	Total	Exam dur.(Hrs)		
	A01	Common Course I – English	64	4	3	15	60	75	2		
	A02	Common Course II – English	80	5	3	15	60	75	2		
	A07	Common Course : Additional	64	4	4	20	80	100	2.5		
1		Language I									
	PHY 1B21	Mechanics I	32	2	2	15	60	75	2		
		Practical I	64	4	-	-	-	-	-		
	MTS 1B21	Basic Calculus	96	6	4	20	80	100	2.5		
	E01	Environment Studies			4**						
		TOTAL		25	16			425			
	A03	Common Course I – English	80	5	4	20	80	100	2.5		
	A04	Common Course II – English	64	4	4	20	80	100	2.5		
	A08	Common Course: Additional	64	4	4	20	80	100	2.5		
2		Language I									
	PHY 2B22	Mechanics II	32	2	2	15	60	75	2		
	PHY 2B23	Practical I	64	4	2	15	60	75	3		
	MTS 2B22	Advanced Calculus	96	6	4	20	80	100	2.5		
	E02	Disaster Management			4**						
		TOTAL		25	20			550			
	A11	General Course	80	5	4	20	80	100	2.5		
	A12	General Course	80	5	4	20	80	100	2.5		
	PHY 3B24	Electrodynamics	48	3	3	15	60	75	2		
3	PHY 3B25	Thermodynamics	48	3	3	15	60	75	2		
		Practical II	32	2	-	-	-	-	-		
	MTS 3B23	Abstract Algebra	64	4	3	15	60	75	2		
	MTS 3B24	Multivariable Calculus	48	3	3	15	60	75	2		
	E03	Human Rights or Intellectual			4**						
		Property Rights or Consumer									
		protection									
		TOTAL		25	20			500			

						M	ax. Ma	arks	
Semester	Code	Name of the course	Total No Contact hours	No of contact hours/Week	Credits	Internal	External	Total	Exam dur.(Hrs)
	A13	General Course	80	5	4	20	80	100	2.5
	A14	General Course	80	5	4	20	80	100	2.5
	PHY 4B26	Statistical Physics, Solid	48	3	3	15	60	75	2
$\parallel 4$		State Physics, Spectroscopy and Photonics							
	PHY 4B27	Electronics (Analog and	48	3	3	15	60	75	2
	-	Digital)							
		Practical III	32	2	-	-	-	-	-
	MTS 4B25	Differential Equations	64	4	3	15	60	75	2
	MTS 4B26	Number Theory	48	3	3	15	60	75	2
	E04	Gender studies or			4**				
		Gerontology							
		TOTAL		25	20			500	
	PHY 5B28	Relativistic Mechanics and	48	3	3	15	60	75	2
		Astrophysics							
	PHY 5B29	Optics	48	3	3	15	60	75	2
5	PHY 5B30	Quantum Mechanics	48	3	3	15	60	75	2
		Practical II	32	2	-	-	-	-	-
		Practical III	32	2	-	-	-	-	-
	MTS 5B27	Complex Analysis	80	5	5	20	80	100	2.5
	MTS 5B28	Real Analysis - I	64	4	4	20	80	100	2.5
		Open Course (offered by	48	3	3	15	60	75	2
		Other Departments)							
		TOTAL		25	21			500	
	PHY 6B31	Nuclear and Particle Physics	48	3	3	15	60	75	2
	PHY 6B32	Elective (Physics Core)	48	3	3	15	60	75	2
	PHY 6B33	Practical II	32	2	2	15	60	75	3
6	PHY 6B34	Practical III	32	2	2	15	60	75	3
	PHY 6B35	Project + Tour Report	32	2	2+1	15	60	75	-
	MTS 6B29	Linear Algebra	80	5	4	20	80	100	2.5
	MTS 6B30	Real Analysis - II	64 48	4	3	15	60	75	2
	MTS 6B31	Elective (Mathematics Core)		3	3	15	60	75	2
	TOTAL			25	23			625	
		Grand Total			120	120			

Tour report shall be evaluated with Practical III

^{*}Credit for practical / project to be awarded only at the end of Semester 2 and Semester 6.

^{**}Mandatory audit courses for the program, but not counted for the calculation of SGPA or CGPA. Student can attain only pass (Grade P) for these courses

Elective Courses (Mathematics Core)

One of the following three courses can be offered in the sixth semester as an elective course under Mathematics Core. (Code MTS 6B31(E01), MTS 6B31(E02) and MTS 6B31(E03)).

							Ma	x. M	arks	
Sl. No	Course Code	Course Title	Semester	Total No. of Contact Hours	Hours/week	Credits	Internal	External	Total Marks	Exam dur.(in Hrs)
1	MTS 6B31(E01)	Numerical Analysis	6	48	3	3	15	60	75	2
2	MTS 6B31(E02)	Introduction to	6	48	3	3	15	60	75	2
		Geometry								
3	MTS 6B31(E03)	Linear Programming	6	48	3	3	15	60	75	2

Elective Courses (Physics Core)

One of the following three courses can be offered in the sixth semester as an elective course under Physics Core (Code PHY 6B32(EL1), PHY 6B32(EL2) and PHY 6B32(EL3))).

							Ma	x. M	arks	
Sl. No	Course Code	Course Title	Semester	Total No. of		Credits	Internal	External	Total Marks	Exam dur.(in Hrs)
1	PHY 6B32(EL1)	Biomedical Physics	6	48	3	3	15	60	75	2
2	PHY 6B32(EL2)	Material Science	6	48	3	3	15	60	75	2
3	PHY 6B32(EL3)	Nanoscience and	6	48	3	3	15	60	75	2
		Technology								

Open Courses

One of the following four courses (MTS 5D01, MTS 5D02, MTS 5D03 and MTS 5D04) can be offered (under Mathematics Core) in the fifth semester as an open course for the students not having Mathematics as Core Course and Mathematics and Physics dual Core programme. The syllabus of these courses were attached in the syllabus of B.Sc. Mathematics programme.

						Ma	ıx. Ma	rks	
Sl. No	Code	Name of the course	Semester	No of contact hours/Week	Credits	Internal	External	Total	Unty. exam Dur. (Hrs)
1	MTS 5D01	Applied Calculus	5	3	3	15	60	75	2
2	MTS 5D02	Discrete Mathematics for Basic	5	3	3	15	60	75	2
		and Applied Sciences							
3	MTS 5D03	Linear Mathematical Models	5	3	3	15	60	75	2
4	MTS 5D04	Mathematics for Decision	5	3	3	15	60	75	2
		Making							

Credit Distribution

Semester	Comm	on course	General	Core	course	Open	Project	
	English	Additional	Course	Mathematics	Physics	course	+	Total
		Language					Tour	
1	3+3	4		4	2	-		16
2	4+4	4		4	2+2*	-		20
3	-	-	4+4	3+3	3+3	-		20
4	-	-	4+4	3+3	3+3	-		20
5		-	-	5+4	3+3+3	3		21
6	-	-	-	4+3+3	3+3+2*+2*	-	2+1	23
Total	14	8	16	39	37	3	3	120

Project and Tour should be offered under Physics Core. Hence total credit under Physics core is 40.

Tour report to be evaluated with Practical Paper III

^{*}Practical

Scheme of Evaluation

The evaluation scheme for each course shall contain two parts: internal evaluation and external evaluation.

Internal Evaluation

20% of the total marks in each course are for internal evaluation. The colleges shall send only the marks obtained for internal examination to the university.

Components of Internal Evaluation

Sl	Components	Marks (For Courses with	Marks (For Courses			
No		Maximum Marks 75)	with Max. Marks 100)			
1	Class Room Participation	3	4			
	(Attendance)					
2	Assignment	3	4			
3	Seminar	3	4			
4	Test paper	6	8			
	Total	15	20			

a) Percentage of Class Room Participation (Attendance) in a Semester and Eligible Internal Marks

ĺ	% of Class Room Participa-	Out of 3 (Maximum internal	Out of 4 (Maximum internal
	tion (Attendance)	marks is 15)	marks is 20)
ĺ	$50\% \le CRP < 75\%$	1	1
ĺ	$75\% \le CRP < 85\%$	2	2
Ī	85% and above	3	4

CRP means % of class room participation (Attendance)

b) Percentage of Marks in a Test Paper and Eligible Internal Marks

Range of Marks in test paper (TP)	Out of 6 (Maximum	Out of 8 (Maximum
	internal marks is 15)	internal marks is 20)
Less than 35%	1	1
$35\% \le TP < 45\%$	2	2
$45\% \le TP < 55\%$	3	3
$55\% \le TP < 65\%$	4	4
$65\% \le TP < 85\%$	5	6
$85\% \le TP \le 100\%$	6	8

Pattern of Question Paper for University Examinations

	For Courses with	Maximum	For Courses with	Maximum			
	External Marks 80	(2.5 Hrs)	External Marks 60 (2 Hrs)				
Section A	Short answer type	Ceiling - 25	Short answer type	Ceiling - 20			
	carries 2 marks each		carries 2 marks each				
	- 15 questions		- 12 questions				
Section B	Paragraph/Problem	Ceiling - 35	Paragraph/Problem	Ceiling - 30			
	type carries 5 marks		type carries 5 marks				
	each - 8 questions		each - 7 questions				
Section C	Essay type carries	$2 \times 10 = 20$	Essay type carries	$1 \times 10 = 10$			
	10 marks (2 out of 4)		10 marks (1 out of 2)				
Total		80		60			

^{*}Questions are to be evenly distributed over the entire syllabus.

Physics Core Course: Practical Evaluation Scheme (60 Marks)

Internal	(15)	External (60)		Marks for
Items	Marks	Items	Marks	Python
				Programming
Record	3	Record with 20 experiments Maxi-	10	10
		mum $1/2$ mark for each experiment		
Regularity	3	Formulae, Theory, Principle/	15	15
in doing the		Program		
experiment				
Attendance	3	Adjustments & setting/ Algorithm	10	12
Test 1	3	Tabulation, Observation and	14	14
		performance/Execution		
Test 2	3	Calculation, result, graph, unit/	8	6
		Result		
		Viva	3	3
Total	15	Total	60	60

SYLLABUS PHYSICS CORE COURSES

Physics Core Courses

$\overline{ ext{Cre}}$	$\operatorname{dit},$	Mark and I	Hour distribution				Ma	x. Ma	arks	
Semester	Sl. No.	Code	Name of the course	Total No	Contact nours No of contact hours/Week	Credits	Internal	External	Total	Exam.dur.(Hrs)
1	1	PHY 1B21	Mechanics I	32	2	2	15	60	75	2
1			Practical I	64	4	-	-	-	-	*
2	2	PHY 2B22	Mechanics II	32	2	2	15	60	75	2
	3	PHY 2B23	Practical I	64	4	2	15	60	75	3
	4	PHY 3B24	Electrodynamics	48	3	3	15	60	75	2
3	5	PHY 3B25	Thermodynamics	48	3	3	15	60	75	2
			Practical II	32	2	-	-	-	-	*
	6	PHY 4B26	Statistical Physics, Solid State	48	3	3	15	60	75	2
4			Physics, Spectroscopy Photonics							
	7	PHY 4B27	Electronics (Analog & Digital)	48	3	3	15	60	75	2
			Practical III	32	2	-	-	-	-	*
	8	PHY 5B28	Relativistic Mechanics and	48	3	3	15	60	75	2
			Astrophysics							
5	9	PHY 5B29	Optics	48	3	3	15	60	75	2
	10	PHY 5B30	Quantum Mechanics	48	3	3	15	60	75	2
			Practical II	32	2	-	-	-	-	*
			Practical III	32	2	-	_	_	-	*
	11	PHY 6B31	Nuclear and Particle Physics	48	3	3	15	60	75	2
	12	PHY 6B32	Elective (Physics Core)	48	3	3	15	60	75	2
			EL1–Biomedical Physics							
$\begin{vmatrix} & & & \\ & 6 & & \end{vmatrix}$			EL2-Material Science							
			EL3-Nanoscience&Technology							
	13	PHY 6B33	Practical II	32	2	2	15	60	75	3
	14	PHY 6B34	Practical III	32	2	2	15	60	75	3
	15	PHY 6B35	Project + Tour Report	32	2	2+1	15	60	75	-
			Grand Total			40				

Tour report shall be evaluated with Practical III

^{*}Credit for practical / project to be awarded only at the end of Semester 2 and Semester 6.

Programme Specific Outcomes Under Physics Core

PSO1 : Understand the basic concepts of fundamentals of mechanics, properties of matter and electrodynamics

PSO2: Understand the theoretical basis of quantum mechanics, relativistic physics, nuclear physics, optics, spectroscopy, solid state physics, astrophysics, statistical physics, photonics and thermodynamics

PSO3: Understand and apply the concepts of electronics in the designing of different analog and digital circuits

PSO4: Understand the basics of computer programming and numerical analysis

PSO5: Apply and verify theoretical concepts through laboratory experiments

Abbreviations used

CL – Cognitive level;

U – understand;

 $\mathbf{Ap} - \mathrm{apply};$

An – analyze;

C – create

KC – Knowledge category;

C – conceptual;

 \mathbf{F} – factual;

 \mathbf{P} – procedural

SEMESTER – 1; Physics Core Course 1

PHY 1B21: MECHANICS – I

2 Credits

2 Hours/Week

	Course Outcome	PSO	CL	KC	Class Sessions
					Allotted
C01	Understand and apply the basic concepts of	PSO1	Ap	С,Р	14
	Newtonian Mechanics to Physical Systems				
C02	Understand and apply the basic idea of work-	PSO1	Ap	С,Р	8
	energy theorem to physical systems				
C03	Understand and apply the rotational dynamics	PSO1	Ap	С,Р	10
	of rigid bodies				

Unit I – Newton's Laws

(14 hrs)

75 Marks[Int: 15 + Ext : 60]

Newton's First Law, Second Law and Third Law – Astronauts in space: Inertial systems and fictitious forces – Standards and units – Some applications of Newton's laws – The astronauts' tug of war, Freight train, Constraints, Block on string, The whirling block, The conical pendulum – The everyday forces of physics – Gravity and Weight; Gravitational force of a sphere; Turtle in an elevator; Gravitational field – Electrostatic force – Contact forces; Block and string; Dangling rope; Whirling rope; Pulleys; Tension and Atomic forces; Normal force; Friction; Block and wedge with friction; Viscosity – Linear restoring force; Spring and block: The equation for simple harmonic motion; Spring and gun: Illustration of initial conditions – Dynamics of a system of particles – The Bola – Centre of mass – Drum major's baton – Centre of mass motion – Conservation of momentum – Spring Gun recoil

[Sections 2.1 to 2.5, 3.1 to 3.3 of An Introduction to Mechanics (1stEdn.) by Daniel Kleppner and Robert J. Kolenkow]

Unit II – Work and Energy

(8 hrs)

Integrating the equation of motion in one dimension – Mass thrown upward in a uniform gravitational field; Solving the equation of simple harmonic motion – Work-energy theorem in one dimension – Vertical motion in an inverse square filed – Integrating the equation of motion in several dimensions – Work-energy theorem – Conical pendulum; Escape velocity – Applying the work-energy theorem – Work done by a uniform force; Work done by a central force; Potential energy – Potential energy of a

uniform force field; Potential energy of an inverse square force – What potential energy tells us about force – Stability – Energy diagrams – Small oscillations in a bound system – Molecular vibrations – Nonconservative forces – General law of conservation of energy – Power

[Sections 4.1 to 4.13 of An Introduction to Mechanics (1stEdn.) by Daniel Kleppner and Robert J. Kolenkow. The problems in chapter 5 should be discussed with this.]

Unit III - Angular Momentum

(10 hrs)

Angular momentum of a particle – Angular momentum of a sliding block; Angular momentum of the conical pendulum – Torque – Central force motion and the law of equal areas – Torque on a sliding block; Torque on the conical pendulum; Torque due to gravity – Angular momentum and fixed axis rotation – Moments of inertia of some simple objects – The parallel axis theorem – Dynamics of pure rotation about an axis – Atwood's machine with a massive pulley – The simple pendulum – The physical pendulum – Motion involving both translation and rotation – Angular momentum of a rolling wheel – Drum rolling down a plane – Work-energy theorem for a rigid body – Drum rolling down a plane : energy method – The vector nature of angular velocity and angular momentum – Rotation through finite angles – Rotation in the xy-plane – Vector nature of angular velocity – Conservation of angular momentum

[Sections 6.1 to 6.7, 7.1, 7.2 and 7.5 of An Introduction to Mechanics (1stEdn.) by Daniel Kleppner and Robert J. Kolenkow]

Books of Study:

1. An Introduction to Mechanics, 1st Edn. – Daniel Kleppner and Robert J. Kolenkow – McGraw-Hill

Reference Books:

1. Berkeley Physics Course: Vol.1: Mechanics, 2ndEdn. – Kittelet al. – McGraw-Hill

Unit/Chapter	Title	Marks
1	Newton's laws	36
2	Work and Energy	18
3	Angular Momentum	25
	79	

^{*}Total marks include that for choice of questions in sections A, B and C in the question paper.

75 Marks[Int: 15 + Ext : 60]

C,P

9

SEMESTER – 2; Physics Core Course 2

PHY 2B22: MECHANICS - II

2 Credits

2 Hours/Week

C04

wave motion

PSO CLKC Class Sessions Course Outcome Allotted C01PSO₁ U \mathbf{C} 7 Understand the features of non-inertial systems and fictitious forces C02Understand and analyze the features of central PSO₁ C,P9 An forces with respect to planetary forces U \mathbf{C} 7 C03Understand the basic ideas of Harmonic PSO₁ oscillator

Unit I – Noninertial Systems and Fictitious Forces (7 hrs)

PSO1

An

Understand and analyze the basic concepts of

Galilean transformations – Uniformly accelerating systems – The apparent force of gravity – Pendulum in an accelerating car – The principle of equivalence – The driving force of the tides – Physics in a rotating coordinate system – Time derivatives and rotating coordinates – Acceleration relative to rotating coordinates – The apparent force in a rotating coordinate system – The Coriolis force – Deflection of a falling mass – Motion on the rotating earth – Weather systems – Foucault's pendulum [Sections 8.1 to 8.5 of An Introduction to Mechanics (1st Edn.) by Daniel Kleppner and Robert J. Kolenkow]

Unit II – Central Force Motion (9 hrs)

Central force motion as a one-body problem – General properties of central force motion – Motion is confined to a plane – Energy and angular momentum are constants of the motion – The law of equal areas – Finding the motion in real problems – The energy equation and energy diagrams – Noninteracting particles – Planetary motion – Hyperbolic orbits – Satellite orbit – Kepler's laws – The law of periods – Properties of the ellipse

[Sections 9.1 to 9.7 of An Introduction to Mechanics (1st Edn.) by Daniel Kleppner and Robert J. Kolenkow]

Unit III – Harmonic Oscillator

(7 hrs)

Introduction and review – Standard form of the solution – Nomenclature – Initial conditions and the frictionless harmonic oscillator – Energy considerations – Time average values – Average energy – Damped harmonic oscillator – Energy and Q-factor – Q factor of two simple oscillators – Graphical analysis of a damped oscillator – Solution of the equation of motion for the undriven damped oscillator – Forced harmonic oscillator – Undamped forced oscillator – Resonance

[Sections 10.1 to 10.3 (except the topic, The Forced Damped Harmonic Oscillator) and Note 10.1 of An Introduction to Mechanics (1stEdn.) by Daniel Kleppner and Robert J. Kolenkow]

What is a wave? – Normal modes and travelling waves – Progressive waves in one direction – Wave speeds in specific media – Superposition – Wave pulses – Motion of wave pulses of constant shape – Superposition of wave pulses – Dispersion; Phase and Group Velocities – Energy in a mechanical wave – Transport of energy by a wave – Momentum flow and mechanical radiation pressure – Waves in two and three dimensions

[Chapter 7 – Progressive Waves (except the topic, The Phenomenon of Cut-off) of Vibrations and Waves by A. P. French]

Books of Study:

- An Introduction to Mechanics, 1stEdn. Daniel Kleppner and Robert J. Kolenkow McGraw-Hill
- 2. Vibrations and Waves A. P. French The M.I.T. Introductory Physics Series CBS Publishers & Distributors

Reference Books:

1. Berkeley Physics Course: Vol.1: Mechanics, 2nd Edn. - Kittel et. al. - McGraw-Hill

Unit/Chapter	Title	Marks
1	Non-inertial systems and fictitious forces	18
2	Central Force Motion	22
3	Harmonic Oscillator	18
4	Waves	21
	79	

^{*}Total marks include that for choice of questions in sections A, B and C in the question paper.

75 Marks[Int: 15 + Ext : 60]

SEMESTER – 3; Physics Core Course 4

PHY 3B24: ELECTRODYNAMICS

3 Credits

3 Hours/Week

PSO CLCourse Outcome KC Class Sessions Allotted CO₁ PSO₁ $_{\rm C,P}$ Understand and analyze the electrostatic prop-An 12 erties of physical systems CO2Understand the mechanism of electric field in PSO₁ U C, P 8 matter U $_{\rm C,P}$ CO3PSO₁ 8 Understand and analyze the magnetic properties of physical systems CO4Understand the mechanism of magnetic field in PSO₁ U $_{\rm C,P}$ 8 matter CO_5 Understand the basic concepts of electrodynam-PSO₁ U C,P12 ics and electromagnetic waves and analyze the

Unit 1 – Electrostatics

properties of electromagnetic waves

(12 hrs)

Electrostatic field – Coulomb's law, Electric field, Continuous charge distributions – Divergence and curl of electrostatic field, Field lines and Gauss's law, The divergence of **E**, Applications of Gauss law, Curl of **E** – Electric potential – Comments on potential, Poisson's equation and Laplace's equation, The potential of a localized charge distribution, Electrostatic boundary conditions – Work and energy in electrostatics, The work done in moving a charge, The energy of point charge distribution.

[Sections 2.1 to 2.4.2 of Introduction to Electrodynamics by David J Griffiths. Additional problems should be done from chapters 1, 2 and 3 of Berkeley Physics Course: Vol.2: Electricity and Magnetism (2nd Edn.) by Edward M Purcell.]

Unit 2 – Electric fields in matter

(8 hrs)

Polarization – Dielectrics, Induced dipoles, Alignment of polar molecules, Polarization – The field of a polarized object, Bound charges, Physical interpretation of bound charges, The field inside a dielectric – The electric displacement – Gauss's law in presence of dielectrics, Boundary conditions

for \mathbf{D} – Linear dielectrics, Susceptibility, Permittivity, Dielectric constant, Boundary value problems with linear dielectrics, Energy in dielectric systems, Forces on dielectrics.

[Sections 4.1 to 4.4 of Introduction to Electrodynamics (4th Edn.) by David J Griffiths. Additional problems should be done from chapter 10 of Berkeley Physics Course: Vol.2: Electricity and Magnetism (2nd Edn.) by Edward M Purcell.]

Unit 3 – Magnetostatics

(8 hrs)

The Lorentz force law – Magnetic fields, Magnetic forces, cyclotron motion, cycloid motion, Currents, Linear, Surface and Volume current density – Biot -Savart law, The magnetic field of steady current – Divergence and curl of B, Straight line currents, Applications of Ampere's law, Magnetic vector potential, Vector potential, Magnetostatic boundary conditions.

[Sections 5.1 to 5.4.2 of Introduction to Electrodynamics (4th Edn.) by David J Griffiths. Additional problems should be done from chapter 6 of Berkeley Physics Course: Vol.2: Electricity and Magnetism (2nd Edn.) by Edward M Purcell.]

Unit 4 – Magnetostatic fields in matter

(8 hrs)

Magnetization – Diamagnets, Paramagnets and Ferromagnets, Torques and forces on magnetic dipoles, Effect of a magnetic field on atomic orbits, Magnetization – Field of a magnetised object, Bound Currents, Physical interpretation of bound currents, Magnetic field inside matter – Auxiliary field **H**, Ampere's law in magnetized materials, Boundary conditions – Linear and nonlinear media, Magnetic susceptibility and permeability, Ferromagnetism.

[Sections 6.1 to 6.4 of Introduction to Electrodynamics (4th Edn.) by David J Griffiths. Additional problems should be done from chapter 11 of Berkeley Physics Course: Vol.2: Electricity and Magnetism (2nd Edn.) by Edward M Purcell.]

Unit 5 – Electrodynamics and Electromagnetic Waves (12 hrs)

Electromotive force – Ohm's law, electromotive force, motional emf – Electromagnetic induction – Faraday's law, induced electric field, inductance, energy in magnetic fields – Maxwell's equations – Electrodynamics before Maxwell, Maxwell's modification of Ampere's law, Maxwell's equations, Magnetic charge, Maxwell's equations inside matter, Boundary conditions – Continuity equation – Poynting's theorem.

Electromagnetic waves in vacuum, Wave equation for \mathbf{E} and \mathbf{B} , monochromatic plane waves in vacuum, energy, and momentum of E.M. waves, Poynting vector.

Sections 7.1 to 7.3, 8.1 and 9.2 to 9.3.1 of Introduction to Electrodynamics by David J Griffiths.

Additional problems should be done from chapter 7 of Berkeley Physics Course: Vol.2: Electricity and Magnetism (2nd Edn.) by Edward M Purcell.]

Books of Study:

- 1. Introduction to Electrodynamics, 4th Edn. David J Griffiths Prentice Hall India Learning Pvt. Ltd.
- 2. Berkeley Physics Course: Vol.2: Electricity and Magnetism, 2nd Edn. Edward M. Purcell McGraw-Hill

Reference Books:

- 1. Electricity and magnetism by Arthur F Kip
- 2. Physics Vol. II by Resnick and Halliday
- 3. Electricity and Magnetism-Hugh D Young and Roger A Freedman
- 4. Electricity and Magnetism by D.N Vasudeva (12threvised edition)
- 5. Electromagnetics by Edminister Schaum's Outline Tata McGraw Hill
- 6. NPTEL video lectures available online

Unit/Chapter	Title	Marks		
1	Electrostatics	20		
2	Electric fields in matter	13		
3	Magnetostatics	13		
4	Magnetostatic fields in matter	13		
5	Electrodynamics and Electromagnetic waves	20		
Total Marks* 79				

^{*}Total marks include that for choice of questions in sections A, B and C in the question paper.

75 Marks[Int: 15 + Ext : 60]

IJ

PSO2

 \mathbf{C}

11

SEMESTER – 3; Physics Core Course 5

PHY 3B25: THERMODYNAMICS

3 Credits

3 Hours/Week

 CO_5

Course Outcome **PSO** CLKC Class Sessions Allotted CO₁ PSO2 U \mathbf{C} 12 Understand the zero and first laws of thermody-CO2U \mathbf{C} 7 Understand the thermodynamics description of PSO2 the ideal gas CO3Understand the second law of thermodynamics PSO₂ U C, P 11 and its applications 7 PSO₂ U \mathbf{C} CO4Understand the basic ideas of entropy

Unit 1 – Zeroth Law and First Law of Thermodynamics (12 hrs)

Understand the concepts of thermodynamic po-

tentials and phase transitions

Macroscopic point of view – Microscopic point of view – Macroscopic versus Microscopic points of view – Scope of Thermodynamics – Thermal equilibrium and Zeroth Law – Concept of temperature – Ideal-Gas temperature – Thermodynamic equilibrium – Equation of state – Hydrostatic systems – Intensive and extensive coordinates – Work – Quasi-static process – Work in changing the volume of a hydrostatic system – PV diagram – Hydrostatic work depends on the path – Calculation of work for quasi-static processes – Work and Heat – Adiabatic work – Internal energy function – Mathematical formulation of First Law – Concept of Heat – Differential form of the First Law – Heat capacity – Specific heat of water; the Calorie – Quasi-static flow of heat; Heat reservoir

[Sections 1.1 to 1.6, 1.10, 2.1 to 2.3, 2.10, 3.1 to 3.6 and 4.1 to 4.8, 4.10 of Heat and Thermodynamics by Zemansky and Dittman]

Equation of state of a gas – Internal energy of a real gas – Ideal gas – Experimental determination of heat capacities – Quasi-static adiabatic process – The microscopic point of view – Kinetic theory of the ideal gas

[Sections 5.1 to 5.5, 5.8 and 5.9 of Heat and Thermodynamics by Zemansky and Dittman]

Unit 3 – Second Law of Thermodynamics

(11 hrs)

Conversion of work into heat and vice versa – Heat engine; Kelvin-Planck statement of the Second Law – Refrigerator; Clausius' statement of the Second Law – Equivalence of Kelvin-Planck and Clausius statements – Reversibility and Irreversibility – Conditions for reversibility – Carnot engine and Carnot cycle – Carnot refrigerator – Carnot's Theorem and corollary – Thermodynamic temperature scale – Absolute zero and Carnot efficiency – Equality of ideal-gas and thermodynamic temperatures

[Sections 6.1, 6.6 to 6.9, 6.14, 7.1 and 7.3 to 7.7 of Heat and Thermodynamics by Zemansky and Dittman]

Unit 4 – Entropy

(7 hrs)

Reversible part of the Second Law – Entropy – Entropy of the ideal gas – TS diagram – Entropy and reversibility – Entropy and irreversibility – Irreversible part of the Second Law – Heat and entropy in irreversible processes – Principle of increase of entropy – Applications of the Entropy Principle – Entropy and disorder – Exact differentials

[Sections 8.1, 8.2, 8.4 to 8.9, 8.11 to 8.14 of Heat and Thermodynamics by Zemansky and Dittman]

Unit 5 – Thermodynamic Potentials and Phase Transitions (11 hrs)

Characteristic functions – Enthalpy – Joule-Thomson expansion – Helmholtz and Gibbs functions – Condition for an exact differential – Maxwell's relations – TdS equations – PV diagram for a pure substance – PT diagram for a pure substance; Phase diagram – First-order phase transitions and Clausius-Clapeyron equation – Clausius-Clapeyron equation and phase diagrams

[Sections 10.1 to 10.6, 9.1, 9.2, 11.3 and 11.4 of Heat and Thermodynamics by Zemansky and Dittman]

Books of Study:

1. Heat and Thermodynamics, 7thEdn. – Mark W. Zemansky and Richard H. Dittman – McGraw-Hill

Reference Books:

1. Classical and Statistical Thermodynamics – Ashley H. Carter – Pearson, 2012

- 2. Basic Thermodynamics Evelyn Guha Narosa, 2002
- 3. Heat and Thermodynamics D. S. Mathur S. Chand Publishers, 2008
- 4. NPTEL video lectures available online

Unit/Chapter	Title	Marks
1	Zeroth Law and First Law of Thermodynamics	20
2	Ideal Gas	12
3	Second Law of Thermodynamic	18
4	Entropy	12
5	Thermodynamic Potentials and Phase Transitions	17
	79	

^{*}Total marks include that for choice of questions in sections A, B and C in the question paper.

75 Marks[Int: 15 + Ext : 60]

SEMESTER – 4; Physics Core Course 6

PHY 4B26: STATISTICAL PHYSICS, SOLID STATE PHYSICS, SPECTROSCOPY & PHOTONICS

3 Credits

3 Hours/Week

	Course Outcome	PSO	CL	KC	Class Sessions
					Allotted
CO1	Understand the basic principles of statistical	PSO2	U	С	14
	physics and its applications				
CO2	Understand the basic aspects of crystallography	PSO2	U	С	13
	in solid state physics				
CO3	Understand the basic elements of spectroscopy	PSO2	U	С	3
CO4	Understand the basics ideas of microwave and	PSO2	U	С	11
	infra red spectroscopy				
CO5	Understand the fundamental ideas of photonics	PSO2	U	\Box C	7

Unit 1 – Statistical Physics

(14 hrs)

Statistical Analysis – Classical versus quantum statistics – Distribution of molecular speeds – Maxwell-Boltzmann distribution – Quantum Statistics – Applications of Bose-Einstein statistics – Blackbody radiation – Applications of Fermi-Dirac statistics

[Sections 10.1 to 10.7 of Modern Physics by Kenneth Krane]

Unit 2 - Solid State Physics

(13 hrs)

Lattice Points and Space Lattice-Basis and crystal structure, unit cells and lattice Parameters, Unit cells versus primitive cells, Crystal systems, Crystal symmetry, Bravais space lattices – Metallic crystal structures – simple cubic, body-centered cubic, face-centered cubic and hexagonal closed packed structure – Other crystal structures – Diamond, Zinc sulphide, Sodium chloride, Caesium chloride – Directions, Planes and Miller indices – Important features of Miller indices – Important planes and directions, distribution of atoms and separation between lattice planes in a cubic crystal – X-Ray diffraction – Bragg's law – Bragg's X-ray spectrometer – Powder crystal method

[Sections 4.1 to 4.7, 4.14 to 4.22 and 5.7 to 5.10 of Solid State Physics by S.O. Pillai]

Unit 3 – Basic Elements of Spectroscopy

(3 hrs)

Quantization of Energy-Regions of Spectrum-Representation of Spectra-Basic Elements of Practical Spectroscopy-Signal to Noise Ratio-Resolving Power-Width and Intensity of Spectral Transitions [Sections 1.2 to 1.7 of Fundamentals of Molecular Spectroscopy by Banwell and McCash]

Unit 4

Microwave Spectroscopy

(5 hrs)

Rotation of molecules – Rotational spectra – Rigid diatomic molecules – Bond length of CO molecule – Intensities of spectral lines

[Sections 2.1 to 2.3.2 of Fundamentals of Molecular Spectroscopy by Banwell and McCash]

Infra Red Spectroscopy & Raman Spectroscopy

(6 hrs)

Energy of a diatomic molecule – Simple harmonic oscillator – Anharmonic oscillator – Morse curve – Selection rules and spectra – The spectrum of HCl – Hot bands – Diatomic vibrating rotator – Born-Oppenheimer approximation

Raman effect – Classical explanation – quantum theory

[Sections 3.1 to 3.2 and 4.1 of Fundamentals of Molecular Spectroscopy by Banwell and McCash]

Unit 5 – Photonics

(7 hrs)

Interaction of light with matter – Absorption, spontaneous emission, stimulated emission, Einstein coefficients – Einstein relations – Light amplification – condition for stimulated emission to dominate spontaneous emission – condition for stimulated emission to dominate absorption – population inversion – metastable states – components of laser – lasing action – types of laser – Ruby laser, NdYAG laser, He-Ne laser, semiconductor laser – Applications – Raman effect – Classical explanation – quantum theory

[Sections 22.4 to 22.9, 22.14, 22.15, 22.19 and 22.20 of Textbook of optics by Brijlal, Subramanium & Avadhanulu]

Books of Study:

- 1. Solid State Physics, 3rd Edn. S. O. Pillai New Age International Pvt. Ltd.
- 2. Fundamentals of Molecular Spectroscopy, 4th Edn. Colin N. Banwell and Elaine M. McCash McGraw-Hill

3. A Text Book of Optics, 25thEdn. – Subrahmanyam and Brijlal, S. Chand & Company Ltd., 2016

Reference Books:

- 1. Solid State Physics by M A Wahab
- 2. Molecular Structure & Spectroscopy by G Aruldhas
- 3. Introduction to Molecular Spectroscopy by G M Barrow
- 4. Raman Spectroscopy by Long D A
- 5. NPTEL video lectures available online

Unit/Chapter	Title	Marks
1	Statistical Physics	23
2	Solid State Physics	21
3	Basic Elements of Spectroscopy	6
4	Microwave Spectroscopy	7
5	Infra Red Spectroscopy	10
6	Photonics	12
	79	

^{*}Total marks include that for choice of questions in sections A, B and C in the question paper.

75 Marks[Int: 15 + Ext : 60]

SEMESTER – 4; Physics Core Course 7

PHY 4B27: ELECTRONICS (ANALOG & DIGITAL)

3 Credits

3 Hours/Week

	Course Outcome	PSO	CL	KC	Class Sessions
					Allotted
CO1	Understand the basic principles of rectifiers and	PSO3	U	С	5
	dc power supplies				
CO2	Understand the principles of transistor	PSO3	U	С	12
CO3	Understand the working and designing of tran-	PSO3	Ap	C, P	11
	sistor amplifiers and oscillators				
CO4	Understand the basic operation of Op – Amp	PSO3	U	С	5
	and its applications				
CO5	Understand the basics of digital electronics	PSO3	II	C	15

Unit 1

1. Semiconductor rectifiers and DC Power supplies (5 hrs)

Preliminaries of rectification- Bridge rectifier- Efficiency- Nature of rectified output- Ripple factor-different types of filter circuits- voltage multipliers- Zener diode- voltage stabilization

[Sections 6.13-6.15, 6.17 - 6.27 of V.K Mehta]

2. Transistors (12 hrs)

Different transistor amplifier configurations:- CB, CE, CC and their characteristics- amplification factors- their relationships- Load line Analysis- Expressions for voltage gain- current gain and power gain of C.E amplifier- cut-off and saturation points- Transistor biasing- Different types of biasing - Base resistor, voltage divider bias method- single stage transistor amplifier circuit- load line analysis-DC and AC equivalent circuits

[Section 8.7 - 8.10, 8.12-8.22, 9.2-9.8, 9.11-9.12, 10.4-10.5, 10.7-10.9 of V K Mehta]

Unit 2

3. Multistage Transistor amplifiers

(4 hrs)

R.C coupled amplifier- frequency response and gain in decibels- Transformer coupled Amplifiers -Direct Coupled Amplifier-Comparison

[Section 11.1-11.8 of VK Mehta]

4. Feedback Circuits and Oscillators

(7 hrs)

Basic principles of feedback-negative feedback and its advantages- positive feedback circuits- Oscillatory Circuits-LC, RC oscillators- tuned collector oscillator- Hartley, Colpitt's, phase shift oscillators - their expressions for frequency

[Sections 13.1-13.5, 14.1 - 14.13 of VK Mehta]

5. Operational amplifier and its applications

5 hrs

Differential amplifier (basic ideas only), OP-amp: basic operation, application, inverting, Non-inverting, summing amplifiers, Differentiator integrator

[Sections 25.1 - 25.5, 25.16, 25.15-25.17,25.23-25.26, 25.32, 25.34-25.35, 25.37 of V K Mehta]

Unit 3

6. Number systems

(5 hrs)

Binary number system, conversions from one system to another (Binary, octal, Hexa decimal), Binary arithmetic, Compliments and its algebra.

(Sections - 2.2 to 2.8 of Aditya P Mathur).

7. Logic gates and circuits

(10 hrs)

Fundamental gates, Universal gates, De Morgan's theorem, Exclusive OR gate, Boolean relations, Half adder, Full adder, RS Flip Flop, JK Flip flop

[Sections - 2.2 to 2.4, 3.1 to 3.5, 5.1 to 5.6, 6.3, 6.4, 7.1, 7.3, 7.5, 7.6, 8.2 Malvino & Leach)

Text books for study:

- 1. Principles of electronics VK Mehta 2008 edition (S. Chand)
- 2. Introduction to Micro Processors Aditya P Mathur (Tata McGarw Hill)

3. Digital principles and applications - Leach and Malvino (Tata McGraw Hill)

Reference Books:

- 1. Electronic Principles by Malvino (Tata McGraw Hill)
- 2. Digital Computer Fundamentals (Thomas. C. Bartee)
- 3. Physics of Semiconductor Devices- Second Edition Dilip K Roy Universities Press
- 4. Digital Fundamentals Thomas L Floyd Pearson Education
- 5. The Art of Electronics-Paul Herowitz & Winfield Hill
- 6. Digital Technology Principles and practice by Virendrakumar
- 7. Electronic Principles and Applications A B Bhattacharya
- 8. NPTEL video lectures available online

Unit/Chapter	Title	Marks			
1	Semiconductor rectifiers and DC Power supplies	9			
2	Transistors	20			
3	Multistage Transistor amplifiers	6			
4	Feedback Circuits and Oscillators	12			
5	Operational amplifier and its applications	9			
6	Number systems	9			
7	Logic gates and circuits	14			
	Total Marks* 79				

^{*}Total marks include that for choice of questions in sections A, B and C in the question paper.

75 Marks|Int: 15 + Ext : 60|

SEMESTER – 5; Physics Core Course 8

PHY 5B28 : RELATIVISTIC MECHANICS AND ASTROPHYSICS

3 Credits

3 Hours/Week

	Course Outcome	PSO	CL	KC	Class Sessions
					Allotted
CO1	Understand the fundamental ideas of special rel-	PSO2	U	С	16
	ativity				
CO2	Understand the basic concepts of general rela-	PSO2	U	С	7
	tivity and cosmology				
CO3	Understand the basic techniques used in astron-	PSO2	U	С	9
	omy				
CO4	Describe the evolution and death of stars	PSO2	U	С	11
CO5	Describe the structure and classification of	PSO2	U	С	5
	galaxies				

Unit 1

1. Special Relativity

(16 hrs)

The need for a new mode of thought – Michelson-Morley experiment – Postulates of Special Relativity – Galilean transformations – Lorentz transformations – Simultaneity – The order of events: Timelike and spacelike intervals – Lorentz length contraction – The orientation of a moving rod – Time dilation – Muon decay – Role of time dilation in an atomic clock - Relativistic transformation of velocity – Speed of light in a moving medium - Doppler effect – Doppler shift in sound – Relativistic Doppler effect – Doppler effect for an observer off the line of motion – Doppler navigation – Twin paradox – Relativistic Momentum and Energy – Momentum – Velocity dependence of the electron's mass – Energy – Relativistic energy and momentum in an inelastic collision – The equivalence of mass and energy – Massless particles – Photoelectric effect – Radiation pressure of light – Photon picture of the Doppler effect – Does light travel at the velocity of light? – The rest mass of the photon – Light from a pulsar

[Sections 11.1 to 11.5, 12.1 to 12.6, 13.1 to 13.4 of An Introduction to Mechanics (1stEdn.) by Daniel Kleppner and Robert J. Kolenkow]

Unit 2

2. General Relativity and Cosmology

(7 hrs)

The principle of equivalence – General theory of relativity – Tests of general relativity – Stellar evolution – Nucleosynthesis – White dwarf stars – Neutron stars – Black holes – The expansion of the universe – Cosmic microwave background radiation – Dark matter – Cosmology and general relativity – The big bang cosmology – Formation of nuclei and atoms – Echoes of the big bang – The future of the universe

[Sections 15.1 to 15.8 and 16.1 to 16.8 of Modern Physics (2ndEdn.) by Kenneth Krane]

Unit 3

3. Basic Tools of Astronomy

(9 hrs)

Stellar distance – Relationship between stellar parallax and distance – Brightness and luminosity – Relationship between Luminosity, brightness and distance – Magnitudes – Apparent magnitude and brightness ratio – Relationship between apparent magnitude and absolute magnitude – Color and temperature of stars – Size and mass of stars – Relationship between flux, luminosity and radius – Star constituents – Stellar spectra – Stellar classification – Hertzsprung-Russell diagram – H-R diagram and stellar radius – H-R diagram and stellar mass

[Sections 1.1 to 1.12 of Astrophysics is Easy: An Introduction for the Amateur Astronomer by Mike Inglis]

4. Stellar Evolution

(11 hrs)

Birth of a Star – Pre-Main-Sequence evolution and the effect of mass – Galactic star clusters – Star formation triggers – The Sun – Internal structure of the sun – Proton-proton chain – Energy transport from the core to the surface – Binary stars – Masses of orbiting stars – Life times of main-sequence stars – Red giant stars – Helium burning – Helium flash – Star clusters, Red giants and the H-R diagram – Post-Main-Sequence star clusters : Globular clusters – Pulsating stars – Why do stars pulsate – Cepheid variables and the period-luminosity relationship – Temperature and mass of Cepheids – Death of stars – Asymptotic giant branch – The end of an AGB star's life – Planetary nebulae – White dwarf stars – Electron degeneracy – Chandrasekhar limit – White dwarf evolution – White dwarf origins – High mass stars and nuclear burning – Formation of heavier elements – Supernova remnants – Supernova types – Pulsars and neutron stars – Black holes

[3.1, 3.2, 3.4 to to 3.15, 3.19 to 3.24 of Astrophysics is Easy: An Introduction for the Amateur Astronomer by Mike Inglis]

5. Galaxies (5 hrs)

Galaxy types - Galaxy structure - Stellar populations - Hubble classification of galaxies - Observing

 $galaxies-spiral, \ barred \ spiral, \ elliptical, \ lenticular \ galaxies-Active \ galaxies \ and \ active \ galactic \ Nuclei \ (AGN)-Gravitational \ lensing-Hubble's \ law-Clusters \ of \ galaxies$

[Sections 4.1 to 4.11 of Astrophysics is Easy: An Introduction for the Amateur Astronomer by Mike Inglis]

Books of Study:

- 1. An Introduction to Mechanics, 1st Edn. Daniel Kleppner and Robert J. Kolenkow McGraw-Hill
- 2. Modern Physics, 2nd Edn. Kenneth S. Krane John Wiley & sons
- 3. Astrophysics is Easy: An Introduction for the Amateur Astronomer Mike Inglis Springer

Reference Books:

- 1. Introduction to Special Relativity Robert Resnick Wiley & Sons
- 2. Special Relativity A P French Viva Books India
- 3. An introduction to Astrophysics BaidyanathBasu, PHI
- 4. Introduction to Cosmology -3rd Edn.-J.V.Narlikar, Cambridge University Press, 2002.
- 5. Principles of Cosmology and Gravitation Michael Berry, Overseas Press, 2005.
- 6. Concepts of Modern Physics Arthur Beiser, Tata McGraw-Hill
- 7. The Big and the Small (Vol II) by G. Venkataraman, Universities Press (India)
- 8. Chandrasekhar and His Limit by G. Venkataramn. Universities Press (India)
- 9. A Brief History of Time by Stephen Hawking, Bantam Books
- 10. NPTEL video lectures available online

Unit/Chapter	Title	Marks
1	Special Relativity	27
2	General Relativity and Cosmology	12
3	Basic Tools of Astronomy	15
4	Stellar Evolution	17
5	Galaxies	8
	79	

^{*}Total marks include that for choice of questions in sections A, B and C in the question paper.

75 Marks[Int: 15 + Ext : 60]

SEMESTER – 5; Physics Core Course 9

PHY 5B29: OPTICS

3 Credits

3 Hours/Week

			T	T	1
	Course Outcome	PSO	CL	KC	Class Sessions
					Allotted
CO1	Understand the fundamentals of Fermat's prin-	PSO2	U	С	5
	ciples and geometrical optics				
CO2	Understand and apply the basic ideas of inter-	PSO2	Ap	C, P	12
	ference of light				
CO3	Understand and apply the basic ideas of diffrac-	PSO2	Ap	C, P	12
	tion of light				
CO4	Understand the basics ideas of polarization of	PSO2	U	С	7
	light				
CO5	Describe the basic principles of holography and	PSO2	U	С	12
	fibre optics				

Unit 1

Fermat's Principle, verification of laws of reflection and refraction

2 hrs

[Sections 2.1 to 2.6 of Brijlal, Subramaniyam, & Avadhanuluand Sections 3.1 to 3.2 of Ajoy Ghatak]

Refraction and reflection by spherical surfaces

3 hrs

Refraction and reflection at a single spherical surfaces. The thin lens, The Principal Foci and Focal length of a lens, The Newton formula, Lateral magnification.

[Sections 4.1 to 4.7 of Ajoy Ghatak]

Unit 2

2. Interference by division of wave front

6 hrs

Superposition of two sinusoidal waves, Interference, coherence, conditions for interference, the interference patterns, intensity distribution. Fresnel's two mirror arrangement, Fresnel's Biprism, Determination of λ and $d\lambda$ of Sodium Light

[Sections 14.1 to 14.4, 14.6 to 14.9 of Brijlal, Subramaniyam, & Avadhanulu, and Sections 14.1 to 14.8 of Ajoy Ghatak. Additional problems should be done from chapter 7 of Introduction to Optics

by Frank.L, Pedrotti, Leno M Pedrotti and Leno S Pedrotti.]

3. Interference by division of amplitude

6 hrs

Interference by a plane film illuminated by a plane wave, cosine law, non reflecting films (the subsections excluded), interference by a film with two nonparallel reflecting surfaces, colours of thin films, Newton's rings, The Michelson interferometer, white light fringes-

[Sections 15.1 to 15.4,15.7, 15.9, 15.11 of Ajoy Ghatak, and Sections 2.1 to 2.6 of Brijlal, Subramaniyam, & Avadhanulu. Additional problems should be done from chapter 7 of Introduction to Optics by Frank.L, Pedrotti, Leno M Pedrotti and Leno S Pedrotti.]

Unit 3

4. Fraunhofer Diffraction

9 hrs

Preliminaries, single slit diffraction pattern, diffraction by circular aperture, limit of resolution, two slit Fraunhofer diffraction pattern, N slit diffraction pattern, plane diffraction grating, resolving power.

[Sections 18.1 to 18.3, 18.5 to 18.8 of Ajoy Ghatak. Additional problems should be done from chapters 11 and 12 of Introduction to Optics by Frank.L,Pedrotti, Leno M Pedrotti and Leno S Pedrotti.]

5. Fresnel Diffraction 3 hrs

Preliminaries, Fresnel half period zones, explanation of rectilinear propagation of light, zone plate [Sections 20.1 to 20.3 of Ajoy Ghatak]

Unit 4 (7 hrs)

6. Polarization

Huygen's explanation of double refraction, positive and negative uniaxial crystals, quarter and half wave plates, types of polarized light, production and analysis of plane, circularly and elliptically polarized light, optical activity, Laurentz half shade polarimeter

[Sections 20.9, 20.17 to 20.20,20.24 of Brijlal, Subramaniyam, & Avadhanulu and corresponding sections of Ajoy Ghatak]

Unit 5 (6 hrs)

7. Holography

Principles of holography, theory of construction and reconstruction of Hologram, Applications of Holography.

[Sections 23.1 to 23.6 of Brijlal, Subramaniyam & Avadhanulu and Sections 21.1 to 21.4 of Ajoy Ghatak]

Unit 6 (6 hrs)

8. Fibre Optics

Optical fibre, Numerical aperture, step index fibre, pulse dispersion, graded index fibre, fibre optic sensors.

[Sections 27.4, 27.7, 27.10, 27.12 of Ajoy Ghatak and corresponding sections from Brijlal, Subramaniyam, & Avadhanulu]

Books of Study:

- 1. Optics by Ajoy Ghatak 4th edition
- 2. Optics by Subramaniam, Brijlal & Avadhanulu 2018(Reprint)
- 3. Introduction to Optics by Frank.L, Pedrotti, Leno M Pedrotti and Leno S Pedrotti

Reference Books:

- 1. Optics Eugine Hetch and A R Ganesan
- 2. Optics by D S Mathur– New edition
- 3. Wave Optics and its Applications Rajpal S Sirohi Orient Longman
- 4. Optical Communications M Mukunda Rao Universities Press
- 5. NPTEL video lectures available online

Unit/Chapter	Title	Marks		
1	Fermat's Principle, verification of laws of reflection	7		
	and refraction Refraction and reflection by spherical			
	surfaces			
2	Interference by division of wave front	9		
3	Interference by division of amplitude	12		
4	Fraunhofer Diffraction	15		
5	Fresnel Diffraction	4		
6	Polarization	12		
7	Holography	9		
8	Fibre Optics	11		
Total Marks*				

^{*}Total marks include that for choice of questions in sections A, B and C in the question paper.

75 Marks[Int: 15 + Ext : 60]

SEMESTER – 5; Physics Core Course 10

PHY 5B30: QUANTUM MECHANICS

3 Credits

3 Hours/Week

	Course Outcome	PSO	CL	KC	Class Sessions
					Allotted
CO1	Understand the particle properties of electro-	PSO2	U	С	7
	magnetic radiation				
CO2	Describe Rutherford – Bohr model of the atom	PSO2	U	С	9
CO3	Understand the wavelike properties of particles	PSO2	U	С	9
CO4	Understand and apply the Schrödinger equation	PSO2	Ap	С,Р	14
	to simple physical systems				
CO5	Apply the principles of wave mechanics to the	PSO2	Ap	С,Р	9
	Hydrogen atom				

Unit I

1. Particle like Properties of Electromagnetic Radiation

7 hrs

Review of electromagnetic waves – Photoelectric effect – Blackbody radiation – Compton effect – Other photon processes – What is a photon?

[Sections 3.1 to 3.6 of Modern Physics by Kenneth Krane]

2. Rutherford-Bohr Model of the Atom

9 hrs

Basic properties of atoms – Thomson model – Rutherford nuclear atom – Line spectra – Bohr model – Frank-Hertz experiment – Correspondence principle – Deficiencies of Bohr model

[Sections 6.1 to 6.8 of Modern Physics by Kenneth Krane]

Unit 2

3. Wavelike Properties of Particles

9 hrs

De Broglie hypothesis - Uncertainty relationships for classical waves - Heisenberg uncertainty relationships - Wave packets - Probability and randomness - Probability amplitude

[Sections 4.1 to 4.6 of Modern Physics by Kenneth Krane]

Unit 3

4. The Schrodinger Equation

14 hrs

Justification of the Schrodinger equation – The Schrodinger recipe – Probabilities and normalization – Applications – Free particle, Particle in a box (one dimension), Particle in a box (two dimensions), Simple harmonic oscillator – Time dependence – Potential energy steps and potential energy barriers

[Sections 5.1 to 5.7 of Modern Physics by Kenneth Krane]

5. Hydrogen Atom in Wave Mechanics

9 hrs

Schrodinger equation in spherical coordinates – Hydrogen atom wave functions – Radial probability densities – Angular momentum and probability densities – Intrinsic spin – Energy levels and spectroscopic notation – Zeeman effect – Fine structure

[Sections 7.1 to 7.8 of Modern Physics by Kenneth Krane]

Books of Study:

1. Modern Physics, 2nd Edn. – Kenneth S. Krane – John Wiley & sons

Reference Books:

- 1. Concepts of Modern Physics, 7th Edn. Arthur Beiser Tata McGraw-Hill
- 2. Modern Physics, 3rd Edn. Raymond A. Serway, Clement J. Moses, Curt A. Moyer Cengage
- 3. Quantum Physics of Atoms, Molecules, Solids, Nuclei & Particles By R.Eisberg & R. Resnick John Wiley
- 4. Modern Physics, 2ndEdn Randy Harris Pearson
- Modern Physics for Scientists and Engineers, 2ndEdn. John R. Taylor, Chris D. Zafiratos, Michael A. Dubson – Prentice-Hall of India Pvt. Ltd.
- 6. Berkeley Physics Course: Quantum Physics by Wichmann
- 7. Theory and Problems in Modern Physics by Gautreau & Savin Schaum's Outlines Series TMH

- 8. Quantum mechanics: Concepts & Applications by Zettilli N, Second Edition, Wiley
- 9. NPTEL video lectures available online

Unit/Chapter	Title	Marks	
1	Particle like Properties of Electromagnetic Radiation	11	
2	Rutherford-Bohr Model of the Atom	15	
3	Wavelike Properties of Particles	15	
4	The Schrodinger Equation	23	
5	Hydrogen Atom in Wave Mechanics	15	
Total Marks*			

^{*}Total marks include that for choice of questions in sections A, B and C in the question paper.

SEMESTER – 6; Physics Core Course 11

PHY 6B31 : NUCLEAR PHYSICS AND PARTICLE PHYSICS

3 Hours/Week 3 Credits 75 Marks[Int: 15 + Ext: 60]

	Course Outcome	PSO	CL	KC	Class Sessions
					Allotted
CO1	Understand the basic aspects of nuclear struc-	PSO2	U	С	12
	ture and fundamentals of radioactivity				
CO2	Describe the different types of nuclear reactions	PSO2	U	C, P	11
	and their applications				
CO3	Understand the principle and working of particle	PSO2	U	C, P	7
	detectors				
CO4	Describe the principle and working of particle	PSO2	U	C, P	7
	accelerators				
CO5	Understand the basic principles of elementary	PSO2	U	С	11
	particle physics				

Unit 1

1. Nuclear Structure and Radioactivity

12 hrs

Nuclear Constituents – Nuclear sizes and shapes – Nuclear masses and binding energies – Liquid drop model – Shell model - Nuclear force – Radioactive decay – Conservation laws in radioactive decay – Alpha decay – Beta decay – Gamma decay – Natural radioactivity – Mossbauer effect

[Sections 12.1 to 12.11 of Modern Physics by Kenneth Krane; Sections 11.5, 11.6 of Beiser]

2. Nuclear Reactions and Applications

11 hrs

Types of nuclear reactions – Radioisotope production in nuclear reactions – Low-energy reaction kinematics – Fission – Fission – Fusion – Fusion processes in stars – Fusion reactors – Applications of nuclear physics – Neutron activation analysis, Medical radiation physics, Alpha decay applications, Synthetic elements

[Sections 13.1 to 13.6 of Modern Physics by Kenneth Krane]

Unit 2

3. Particle Detectors 7 hrs

Particle Detectors – Wilson Cloud Chamber – Bubble Chamber – Ionization Chambers – Proportional Counter – Geiger-Muller Counter – Scintillation Counters and Semiconductor Counters – Spark Chamber – Cerenkov Counter – Neutron Counting – The Photographic Plate.

[Sections 17.1 to 17.11of Atomic and Nuclear Physics – An Introduction by Littlefield and Thorley]

4. Particle Accelerators

7 hrs

Particle Accelerators – Cockcroft-Walton Proton Accelerator – Van de Graaff Electrostatic Generator – Linear Accelerator – Lawrence Cyclotron – Synchrocyclotron – Electron Accelerating Machines : Betatron– Electron Synchrotron – Proton Synchrotron – Alternating-Gradient Synchrotron – Intersecting Beam Accelerators – The Growth and Future of Large Accelerating Machines

[Sections 18.1 to 18.12 of Atomic and Nuclear Physics – An Introduction by Littlefield and Thorley]

Unit 3

5. Elementary Particles

11 hrs

The four basic forces – Particles and antiparticles – Families of particles – Conservation laws – Particle interactions and decays – Resonance particles – Energetics of particle decays – Energetics of particle reactions – The Quark Model – The Standard Model

[Sections 14.1 to 14.9 of Modern Physics by Kenneth Krane]

Books of Study:

- 1. Modern Physics, 2ndEdn. Kenneth S. Krane John Wiley & sons
- 2. Atomic and Nuclear Physics An Introduction, 3rdEdn. T.A. Littlefield and N. Thorley Springer
- 3. Concepts of Modern Physics, 7thEdn. Arthur Beiser Tata McGraw-Hill

Reference Books:

- 1. Modern Physics, 3rdEdn. Raymond A. Serway, Clement J. Moses, Curt A. Moyer Cengage
- 2. Quantum Physics of Atoms, Molecules, Solids, Nuclei & Particles By R.Eisberg & R. Resnick John Wiley

- 3. Theory and Problems in Modern Physics by Gautreau & Savin Schaum's Outlines Series TMH
- 4. Modern Physics for Scientists and Engineers, 2ndEdn. John R. Taylor, Chris D. Zafiratos, Michael A. Dubson Prentice-Hall of India Pvt. Ltd
- 5. Modern Physics, 2ndEdn Randy Harris Pearson
- 6. A practical approach to Nuclear Physics, 1st Edition, K. Muraleedhara Varier- Narosa Publishing House
- 7. NPTEL video lectures available online

Mark Distribution for Setting Question Paper

Unit/Chapter	Title	Marks			
1	1 Nuclear Structure and Radioactivity				
2	Nuclear Reactions and Applications	18			
3	Particle Detectors	12			
4	Particle Accelerators	12			
5	Elementary Particles	17			
Total Marks*					

^{*}Total marks include that for choice of questions in sections A, B and C in the question paper.

ELECTIVE COURSES

SEMESTER – 6; Physics Core Course 12 (Elective)

PHY 6B32 (EL1): BIOMEDICAL PHYSICS

3 Hours/Week

3 Credits 75 Marks[Int: 15 + Ext: 60]

	Course Outcome	CL	KC	Class Sessions
				Allotted
CO1	Understand the basic principles of biophysics	U	С	12
CO2	Understand the fundamentals of medical instru-	U	С	10
	mentation			
CO3	Understand the principles of ultrasound and x-	U	C	9
	ray imaging			
CO4	Understand the basic principles of NMR	U	C	9
CO5	Describe the applications of lasers in medicine	U	С	8

Unit I – Physical foundations of biophysics

(12 hrs)

Free energy, Internal energy, Thermodynamics and Statistical mechanics, Reaction kinetics.

(Sections 4.1 to 4.4 from "Biophysics: An Introduction" by Rodney Cotterlie, Wiley.)

Transport Processes: Diffusion, Osmosis, Surface tension, Viscosity, thermal conduction.

(Sections 5.1 to 5.3 from "Biophysics: An Introduction" by Rodney Cotterlie, Wile.

Oxidation and reduction, redox potential, examples of redox potential in biological systems.

Sections 4.5 and 9.3 from "Biophysics: An Introduction" by Rodney Cotterlie, Wiley.

Membrane Physics: Diffusion through cell membrane, factors affecting diffusion, Membrane potentials: Resting potentials, action potentials, Hodgkin-Huxley model for membrane transport. Donnan equilibrium, Goldman equation.

(Sections 11.1, 11.2, 12.1, 12.2 from "Biophysics: An Introduction" by Rodney Cotterlie, Wiley. Also refer: Principles of Biomedical engineering by Sundararajan V Madihally, Artech house.

Unit 2 – Fundamentals of medical instrumentation (10 hrs)

Physiological systems of the body, sources of biomedical signals, basic medical instrumentation systems, performance, constraints and regulations, intelligent medical instrumentation systems. Origin of bioelectric signals, ECG, EEG, EMG. Recording electrodes and microelectrodes. Transducers and biosensors.

(Sections 1.1 to 1.8, 2.1 to 2.8 & 3.1 to 3.10 from "Handbook of Biomedical Instrumentation", R S Khandpur, Tata Mcgraw Hill)

Unit 3 – Ultrasound and X ray medical imaging systems (9 hrs)

Ultrasonic Imaging-properties of ultrasound, modes of ultrasound transmission-pulsed, continuous, pulsed Doppler, ultrasound imaging, ultrasonic diagnosis, ultrasonic transducers.

(Sections 9.2, 9.3 from Leslie Cromwell, "Biomedical Instrumentation and measurement", Prentice hall of India, New Delhi)

X-rays- Instrumentation for diagnostic X-rays, visualization of X-rays-flouroscopy, X-ray filters, X-ray films, Image intensifiers, Special technique-grid, contrast media, Angiography.

(Sections 14.1 to 14.3 from Leslie Cromwell, "Biomedical Instrumentation and measurement", Prentice hall of India, New Delhi)

X-ray computed tomography – Computed tomography, basic principle, contrast scale, system components-scanning system, processing unit, viewing part, storage unit, Helical CT scanner.

(Sections 20.1, 20.2 from Handbook of Biomedical Instrumentation by R S Khandpur, Tata Mc GrawHill)

Unit 4 – Nuclear medical imaging systems (9 hrs)

Nuclear Medical imaging systems-radio isotopes in medical imaging systems, physics of radioactivity, uptake monitoring equipment, radioisotope rectilinear scanner, gamma camera, Emission computed tomography, Positron emission tomography (PET Scanner)

(Sections 21.1, 21.2 from Handbook of Biomedical Instrumentation by R S Khandpur, Tata Mc GrawHill)

Principles of NMR, Image reconstruction techniques, Basic NMR components, Biological effects of NMR imaging, advantages of NMR imaging.

(Sections 22.1, 22.2, 22.3, 22.4, 22.5 from Handbook of Biomedical Instrumentation by R S Khandpur, Tata Mc GrawHill Publications)

(Reference- Medical Imaging Physics, William Hendee, John Wiley and Sons Publications)

Unit 5 – Lasers in medicine (8 hrs)

Special properties of laser beam (coherence, collimation, monochromaticity), laser active medium, focal length of the laser lens, Laser-tissue interactions, Basic principles of Nd-YAG, CO2, and Argon Lasers, An overview of their clinical applications with special reference to Gynecology, pulmonary, neurosurgery, dermatology, ophthalmology. Photodynamic therapy, Laser safety measures.

(Sections of Chapter 1, Chapter 2, Chapter 3, Chapter 5 from Lasers in Medicine - An Introductory Guide, Gregory Absten, Springer Science Publications)

Books of Study:

- 1. Biophysics: An Introduction by Rodney Cotterlie, Wiley
- 2. Handbook of Biomedical Instrumentation, R S Khandpur, Tata Mcgraw Hill
- 3. Biomedical Instrumentation and measurement, Leslie Cromwell, Prentice hall of India
- 4. Lasers in Medicine An Introductory Guide, Gregory Absten, Springer Science

Reference Books:

- 1. Medical Physics by J R Cameron and J G Skofonick, Wiley Eastern)
- 2. The physics of medical imaging by S Webb, Hilger Publications
- 3. Techniques for radiation dosimetry by K Mahesh and D R Vij, Wiley Eastern Limited
- 4. Clinical nuclear medicine by Maisey, Britton, Chapman and Hall
- 5. Ultra sound in Medicine, by F Duck, IOP Publications
- 6. Medical Instrumentation Application and Design, by John G. Webster, John Wiley and sons, New York
- 7. Introduction to Biomedical equipment technology, John M. Brown, John Wiley and sons, New York
- 8. Medical Imaging Physics, W.R.Hendee & E.R.Ritenour, (3rd eds), Mosbey Inc.,

Mark Distribution for Setting Question Paper

Unit/Chapter	Title	Marks		
1	1 Physical foundations of biophysics			
2	2 Fundamentals of medical instrumentation			
3	3 Fundamentals of medical instrumentation			
4	Nuclear medical imaging systems	15		
5	Lasers in medicine	13		
Total Marks*				

^{*}Total marks include that for choice of questions in sections A, B and C in the question paper.

SEMESTER – 6; Physics Core Course 12 (Elective)

$\begin{array}{c} \text{PHY 6B32 (EL2): NANOSCIENCE AND} \\ \text{TECHNOLOGY} \end{array}$

3 Hours/Week

3 Credits 75 Marks[Int: 15 + Ext: 60]

	Course Outcome	CL	KC	Class Sessions
				Allotted
CO1	Understand the elementary concepts of	U	С	5
	nanoscience			
CO2	Understand the electrical transport mechanisms	U	С	9
	in nanostructures			
CO3	Understand the applications of quantum me-	U	C	12
	chanics in nanoscience			
CO4	Understand the fabrication and characterization	U	C	17
	techniques of nanomaterials			
CO5	Enumerate the different applications of nan-	U	С	5
	otechnology			

Unit I – Introduction:

(5 hrs)

Length scales in Physics- nanometer- Nanostructures: Zero, One Two and Three dimensional nanostructures (Chapter 3, Text 2)

Band Structure and Density of State at nanoscale: Energy Bands, Density of States at low dimensional structures. (Chapter 3, Text 1)

Unit 2 – Electrical transport in nanostructure (9 hrs)

Electrical conduction in metals, The free electron model. Conduction in insulators/ionic crystals - Electron transport in semiconductors - Various conduction mechanisms in 3D (bulk), 2D(thin film) and low dimensional systems: Thermionic emission, field enhanced thermionic emission (Schottky effect), Field assisted thermionic emission from traps (Poole-Frenkel effect), Arrhenius type activated conduction, Variable range, Hopping conduction, Polaron conduction. (Chapter 4, Text 1)

Unit 3 –Introductory Quantum Mechanics for Nanoscience: (12 hrs)

Size effects in small systems, Quantum behaviors of nanometric world: Applications of Schrodinger equation - infinite potential well, potential step, potential box; trapped particle in 3D (nanodot), electron trapped in 2D plane (nanosheet), electrons moving in lD (nanowire, nanorod, nanobelt), Excitons, Quantum confinement effect in nanomaterials (Chapter 5, Text 1)

Unit 4 - Growth techniques of nanomaterials (Elementary ideas only) (8 hrs)

Top down vs bottom up techniques, Lithographic process, Non Lithographic techniques: Plasma arc discharge, sputtering. Evaporation: Thermal evaporation, Electron beam evaporation, Chemical Vapour Deposition (CVD), Pulsed Laser Deposition, Molecular Beam Epitaxy, Sol-Gel Technique, Electro-deposition., Ball-milling.

(Chapter 6, Text.1: Sections 6.1, 6.2. 6.3, 6.4.1, 6.4.2, 6.4.2.1, 6.4.3, 6.4.3.1. 6.4.3.2, 6.4.4, 6.4.5, 6.4.6,6.4.7,6.4.8,6.4.9)

Unit 5 – Characterisation tools of nanomaterials (9 hrs)

Scanning Probe Microscopy (SPM): Basic Principles of SPM techniques, details of STM, tunneling current, local barrier height, local density of states. Some applications of STM.

(Section 7.1.1- 7.1.3.3, 7.1.3.5, Text 1), General concepts of AFM (Section 7.2.1 - 7.2.4, Text-1), Electron microscopy (7.3.1-7.3.6, Text -1).

Unit 6 - Applications of nanotechnology (Elementary ideas only) (5 hrs)

Buckminster fullerene, Carbon nanotube, nano diamond, BN Nanotube, Nanoelectronics - single electron transistor (no derivation), Molecular machine, Nanobiomatrics (Chapter 8, Text 1). Applications of nanomaterials in energy, medicine and environment (Text 2)

Books of Study:

- 1. Introduction to Nanoscience & Nanotechnology by K. K. Chattopadhyaya and A. N. Banerjee, Publisher: PHI Learning and Private Limited
- 2. Nanotechnology, Rakesh Rathi, S Chand & Company, New Delhi

Reference Books:

- 1. Nanoparticle Technology Handbook- M. Hosokawa, K. Nogi, M. Naita, T. Yokoyama (Eds.), Elsevier 2007
- Encyclopaedia of Materials Characterization, Surfaces, Interfaces, Thin Films, Eds. Brundle, Evans and Wilson, Butterworth- Heinmann, 1992
- 3. Springer Handbook of nanotechnology, Bharat Bhushan (Ed.), Springer-Verlag, Berlin, 2004
- 4. Nano Science and Technology, VS Muraleedharan and A Subramania, Ane Books Pvt. Ltd, New Delhi
- 5. A Handbook on Nanophysics, John D, Miller, Dominant Publishers and Distributors, Delhi-51

- 6. Introduction to Nanotechnology, Charles P Poole Jr. and Frank J Owens, Wiley Students Edition
- 7. Nano-and micro materials, K Ohno et. A Springer International Edition 2009, New Delhi

Mark Distribution for Setting Question Paper

Unit/Chapter	Title	Marks
1	Introduction	9
2	Electrical transport in nanostructure	15
3	Introductory Quantum Mechanics for Nanoscience	19
4	Growth techniques of nanomaterials	12
5	Characterisation tools of nanomaterials	15
6	Applications of nanotechnology	9
	Total Marks*	79

^{*}Total marks include that for choice of questions in sections A, B and C in the question paper.

SEMESTER – 6; Physics Core Course 12 (Elective)

PHY 6B32 (EL3): MATERIALS SCIENCE

3 Hours/Week

 $3 \text{ Credits} \quad 75 \text{ Marks}[\text{Int: } 15 + \text{Ext: } 60]$

	Course Outcome	CL	KC	Class Sessions
				Allotted
CO1	Understand the basic ideas of bonding in materials	U	С	6
CO2	Describe crystalline and non crystalline materials	U	C	7
CO3	Understand the types of imperfections nad diffusion	U	С	11
	mechanisms in solids			
CO4	Describe the different properties of ceramics and	U	С	13
	polymers			
CO5	Describe the different types of material analysis	U	С	11
	techniques			

Unit 1 (13 hrs)

Introduction: What is material science, Classification of materials-metals, ceramics, polymers, composites, Advanced materials, smart materials.

(Section 1.1 to 1.6 of Callister's Material science and Engineering)

Bonds in materials: Atomic bonding in solids-bonding forces and energies, Primary bonding - Ionic bonding, Covalent bonding, metallic bonding, Secondary bonding- van der waals bonding, fluctuating induced dipole bonds, polar molecule induced dipole bonds, permanent dipole bonds example of anomalous volume expansion of water.

(Section 2.5 to 2.8 of Callister's Material science and Engineering)

Crystals: Crystalline and Non Crystalline materials -Single crystals, polycrystals, Anisotropy, metallic crystal structures, atomic packing factors of FCC, BCC, Hexagonal close packed crystal structure, Density computations, Linear and planar densities, polymorphism and allotropy, non crystalline solids.

(Section 3.8 to 3.11, 4.2 to 4.9 of Callister's Material science and Engineering)

Unit 2 (11 hrs)

Imperfections in Solids: Point defects, Vacancies and selfinterstitials, substitutional impurities, atomic point defects-Schottky defect, Frenkel defect, Dislocations-edge and screw dislocations, burgers vector, Interfacial defects-External surfaces, Grain boundaries, twin boundaries, stacking faults, Bulk and volume defects.

(Section 5.2 to 5.8 of Callister's Material science and Engineering)

Diffusion in solids : Introduction, Diffusion mechanism, Vacancy diffusion, Interstitial diffusion, Steady state diffusion and Non-steady state diffusion, fick's laws, Factors that influence diffusion-temperature, diffusion species, example of aluminium for IC interconnects. diffusion in ionic and polymeric materials

(section 6.1 to 6.8 of Callister's Material science and Engineering)

Unit 3
$$(13 \text{ hrs})$$

Ceramics and its properties: Glasses, Glass ceramics, properties, refractories -fire clay and silica refractories, Abrasives, cements, advanced ceramics-optical fibers, ceramic ball bearings, piezo electric ceramics, stress-strain behaviour of ceramics, flexural strength and elastic behaviour.

(Section 12.1 to 12.8, 12.11 of Callister's Material science and Engineering)

Polymers and its properties: Different forms of Carbon-Diamond, Graphite, Fullerenes, Carbon nano tubes. (Qualitative aspects only)

(Section 4.17 of Callister's Material science and Engineering)

Hydro carbon molecules, polymer molecules, homo polymers and copolymers, molecular weight calculation, linear polymers, branched polymers, cross linked polymers, network polymers, thermo setting and thermo plastic polymers, stress-strain behaviour and viscoelastic deformation of polymers.

(Section 13.1 to 13.9, 14.2, 14.3, 14.4 of Callister's Material science and Engineering)

Material Analysis Techniques: Single crystal and powder diffraction techniques with diffractometer, Laue's technique and rotating crystal method, Microscopic techniques-Optical microscopy, electron microscopy, transmission electron microscopy, scanning electron microscopy, Scanning probe microscopy, construction and working of each device, Grain size determination technique.

(Section 4.20, 5.12, 5.13 of Callister's Material science and Engineering)

Books of Study:

1. 1. Material Science and Engineering by William D. Callister, Adapted by R. Balasubramanyam (IIT, Kanpur), Published by Wiley India Pvt Ltd (Reprint 2011)

Reference Books:

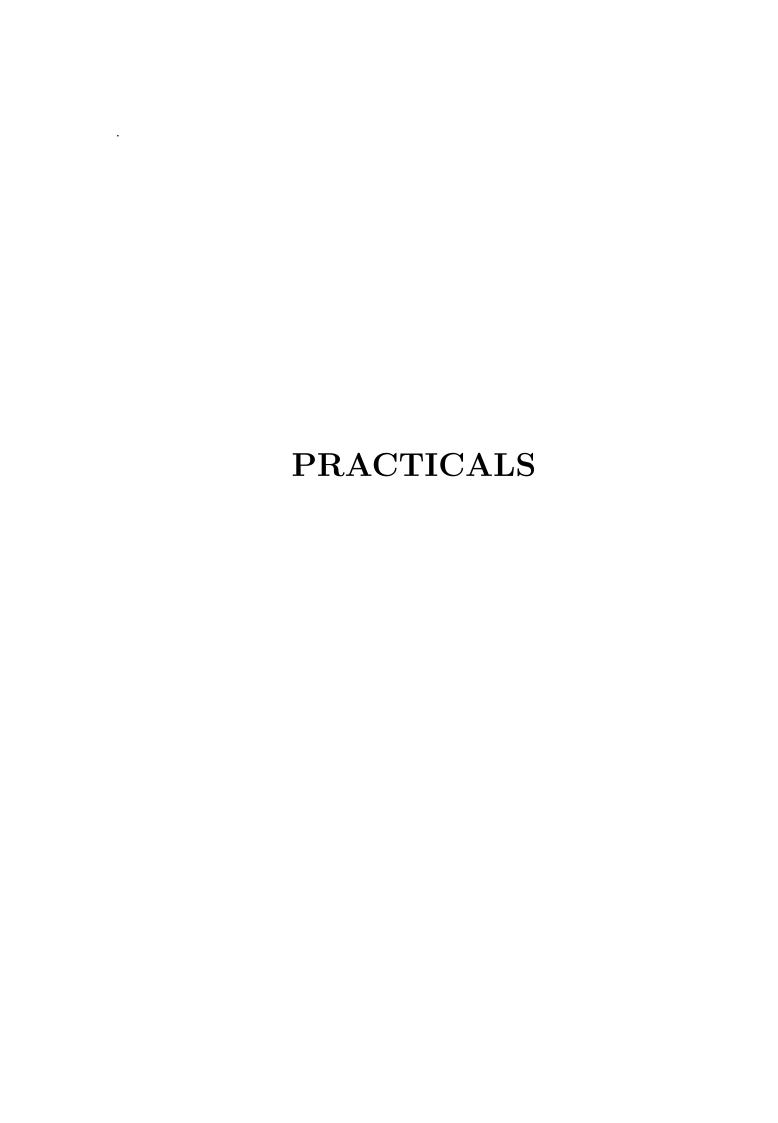
- 1. Materials science and engineering- Vth Edn- V Raghavan (PHI)
- 2. Material science by S.L.Kakani & Amit Kakani, 2nd edition 2010, reprint 2011

- 3. Material Science & Engineering, R.K. Rajput (Jain Book Agency)
- 4. Material Science and Engineering, I. P. Singh, & Subhash Chander (Jain Book Agency)

Mark Distribution for Setting Question Paper

Unit/Chapter	Title	Marks		
1	Unit 1	22		
2	Unit 2	18		
3	Unit 3	22		
4	Unit 4	17		
Total Marks*				

^{*}Total marks include that for choice of questions in sections A, B and C in the question paper.



Dual Core Physics Practical Syllabus

All centres must arrange sufficient number of apparatus before the practical examination. All apparatus must be in proper condition before the practical examination.

The external practical examination will be conducted at the end of **second** and **sixth** semesters. At the time of external examination, a student has to produce **certified fair record** with a minimum of **75**% of the experiments, listed in the syllabus. Valuation of the record must be done internally and externally. **A maximum of 1/2 mark can be awarded to an experiment which is neatly recorded**. Total mark for record in external valuation is 10. The principle or the logic and the relevant expressions of the experiment must be shown at the time of examination.

Two test papers for practical internals could be conducted by including test papers in any two convenient cycles in the place of an experiment. A batch of students can be evaluated in each class. If there are a total of 4 cycles for a practical course, a test paper each can be included in the 3rd and 4th cycles. If there are a total of 3 cycles for a practical course, a test paper each can be included in the 2nd and 3nd cycles. A model examination can also conducted after completion of all cycles. Internal grade for test papers can be awarded based on the best two performances. Digital balance is allowed for mass measurements.

Number of questions in the question paper shall be 8 for Paper I & II: and 6 from Electronics & 2 from Python programs for PAPER- III: out of these a minimum of 75% of the questions are to be set for the examination at a centre.

SEMESTER 1 to 2: Physics Core Course 3

PHY2 B23: PRACTICAL I

4 Hours/Week in each Semester

2 Credits

	Course Outcome	CL	KC	Class Sessions
				Allotted
CO1	Apply and illustrate the concepts of properties	Ap	P	32
	of matter through experiments			
CO2	Apply and illustrate the concepts of electricity	Ap	P	32
	and magnetism through experiments			
CO3	Apply and illustrate the concepts of optics	Ap	P	32
	through experiments			
CO4	Apply and illustrate the principles of electronics	Ap	P	32
	through experiments			

(Any 20 experiments)

- 1. Young's modulus-non uniform bending-using pin and microscope-(load-extension graph)
- 2. Young's modulus-Uniform bending-using optic lever
- 3. Moment of inertia-Flywheel (Calculate percentage error and standard deviation)
- 4. Moment of Inertia-Torsion Pendulum
- 5. Rigidity modulus-static torsion
- 6. Compound pendulum-acceleration due to gravity, Radius of gyration
- 7. Katers pendulum- Acceleration due to gravity
- 8. Liquid lens-Refractive index of liquid and glass -a) determine R using a)water& b) Buoy's method
- 9. Spectrometer-solid prism-Refractive index of the material of the prism, measuring angle of minimum deviation
- 10. Spectrometer-solid prism- Dispersive power
- 11. a. Searle's vibration magnetometer- ratio of moments b. Searle's and box type vibration magnetometers-m & Bh.
- 12. Melde's string arrangement-Frequency, relative density of liquid and solid (both modes)

- 13. Mirror Galvanometer-figure of merit
- 14. Potentiometer-calibration of ammeter
- 15. Ballistic Galvanometer- BG constant using HMS-then find Bh.
- 16. Ballistic galvanometer-Comparison of capacitance- Desauty's method
- 17. Spectrometer- i-d curve
- 18. Verification of Thevenin's theorem and maximum power transfer theorem
- 19. Lissajous figures Measurement of frequency and phase shift of sinusoidal signals using CRO
- 20. Cantilever -scale and telescope /pin and microscope
- 21. Single slit diffraction using LASER
- 22. Determination of dielectric constant of liquid/thin sheet
- 23. Thermo emf measurement using digital multimeters study of Seebeck effect
- 24. Thermal conductivity of a good conductor by Searle's method.

Books of Study:

- 1. Electronics lab manual- K A Navas (vol 1 & 2)
- 2. B.Sc Practical Physics- C L Arora
- 3. Practical Physics- S L Gupta V Kumar

Reference Books:

1. Advanced Practical Physics for students – B L Worksnop and H T Flint

SEMESTER 3, 5 and 6: Physics Core Course 13

PHY 6B33: PRACTICAL II

2 Hours/Week in each Semester

2 Credits

	Course Outcome	CL	KC	Class Sessions
				Allotted
CO1	Apply and illustrate the concepts of properties	Ap	P	24
	of matter through experiments			
CO2	Apply and illustrate the concepts of electricity	Ap	P	24
	and magnetism through experiments			
CO3	Apply and illustrate the concepts of optics and	Ap	P	24
	spectroscopy through experiments			
CO4	Apply and illustrate the principles of heat	Ap	P	24
	through experiments			

(Any 20 experiments)

- 1. e/m measurement –Thomson's apparatus
- 2. Spectrometer-Cauchy's constants
- 3. Spectrometer- Diffraction Grating-Normal incidence
- 4. Spectrometer- Diffraction Grating-minimum deviation
- 5. Spectrometer $i_1 i_2$ curve
- 6. Laser-wavelength using transmission grating
- 7. Spectrometer-Quartz prism-Refractive indices of quartz for the ordinary and extra ordinary rays
- 8. Newton's rings-wavelength of sodium light
- 9. Air wedge-angle of the wedge, radius of a thin wire
- 10. Lee's Disc –thermal conductivity of a bad conductor
- 11. Potentiometer-calibration low range and high range voltmeters
- 12. Potentiometer- Reduction factor of TG
- 13. Variation of field with distance-Circular coil-moment of magnet & Bh
- 14. Resolving power of grating

- 15. Carey Foster's bridge-Temperature coefficient of Resistance
- 16. Conversion of Galvanometer to voltmeter and calibrating using Potentiometer. (Plot Using software)
- 17. Conversion of Galvanometer to ammeter and calibrating using Potentiometer.
- 18. BG Absolute Capacity
- 19. BG-High resistance by leakage method
- 20. Dispersive power of grating
- 21. Planck's constant using LED's (Minimum 4 nos.)
- 22. Polarimeter-Specific rotation of sugar solution
- 23. Numerical aperture of an optical fibre by semiconductor laser
- 24. Frequency of AC using Sonometer

Books of Study:

- 1. Electronics lab manual K A Navas (vol 1 & 2)
- 2. B.Sc Practical Physics C L Arora
- 3. Practical Physics S L Gupta V Kumar

Reference Books:

- 1. Advanced Practical Physics for students B L Worksnop and H T Flint
- A practical approach to Nuclear Physics, 1st Edition, K. Muraleedhara Varier- Narosa Publishing House

SEMESTER 4 to 6: Physics Core Course 14

PHY 6B34: PRACTICAL III

2 Hours/Week in each Semester

2 Credits

	Course Outcome	CL	KC	Class Sessions
				Allotted
CO1	Apply and illustrate the principles of semi-	Ap	P	24
	conductor diode and transistor through exper-			
	iments			
CO2	Apply and illustrate the principles of transistor	Ap	Р	24
	amplifier and oscillator through experiments			
CO3	Apply and illustrate the principles of digital	Ap	Р	24
	electronics through experiments			
CO4	Analyze and apply computational techniques in	Ap	Р	24
	Python programming			

Unit I: (Any 15 experiments)

- 1. Construction of full wave a) Centre tapped and b) Bridge rectifiers
- 2. Characteristics of Zener diode and construction of Voltage regulator.
- 3. Transistor input, output & transfer characteristics in Common Base Configuration and calculation of current gain.
- 4. Transistor input, output & transfer characteristics in Common emitter Configuration and calculation of current gain
- 5. CE Transistor Amplifier-Frequency response. (Design the circuit for a given collector current IC)
- 6. Negative feedback amplifier
- 7. Half adder using NAND gates
- 8. Full adder using NAND gates-construction & verification
- 9. LC Oscillator (Hartley or Colpitt's)
- 10. Phase shift oscillator
- 11. Operational Amplifier –inverting, non inverting, Voltage follower

- 12. LCR circuits-Resonance using CRO
- 13. Construction of basic gates using diodes (AND, OR) & transistors (NOT), verification by measuring voltages
- 14. Voltage multiplier (doubler, Tripler) (Connections to be realized through soldering. The desoldering has to be carried out at the end of the experiment.)
- 15. Multivibrator using transistors.
- 16. Flip-Flop circuits –RS and JK using IC's
- 17. Verification of De-Morgan's Theorem using basic gates.
- 18. Photo diode V-I characteristics. Determine quantum efficiency and responsivity of the PD
- 19. Study the characteristics of LED (3 colours) and LDR.
- 20. Wave shaping R-C circuits -integrator and differentiator
- 21. OPAMP- adder, subtractor

Unit II: Numerical Methods Using Python: Minimum 5 programs to be done

- 1. Solution of equations by bisection and Newton-Raphson methods
- 2. Least square fitting straight line fitting.
- 3. Numerical differentiation using difference table.
- 4. Numerical Integration Trapezoidal and Simpson's 1/3 rd rule.
- 5. Taylor series $\sin \theta$, $\cos \theta$
- 6. Solution of 1st order differential equation Runge Kutta method
- 7. Simulation of freely falling body. Tabulation of position, velocity and acceleration, as function of time.
- 8. Simulation of projectile Tabulation of position, velocity and acceleration as a function of time –Plot trajectory in graph paper from tabulated values.

Books of Study:

- 1. Electronics lab manual K A Navas (vol 1 & 2)
- 2. B.Sc Practical Physics C L Arora
- 3. Practical Physics S L Gupta V Kumar

- 4. Computational Physics, V.K. Mittal, R.C. Verma & S.C. Gupta-Published by Ane Books
- $5.\$ Introductory methods of numerical analysis, S.S.Shastry , (Prentice Hall of India,1983)
- 6. Introduction to Python for Engineers and Scientists by Dr.Sandeep Nagar, Apress publications.
- 7. Python for Education by Dr. B P Ajithkumar, IUAC, New Delhi; e-book freely downloadable from www.expeyes.in/documents/mapy.pdf

Reference Books:

1. Advanced Practical Physics for students – B L Worksnop and H T Flint

SEMESTER 6 : Physics Core Course 15

PHY 6B35: PROJECT

2 Hours/Week 2 Credits

	Course Outcome	CL	KC	Class Sessions
				Allotted
CO1	Understand research methodology	U	P	08
CO2	Understand and formulate a research project	C	P	08
CO3	Design and implement a research project	С	Р	08
CO4	Identify and enumerate the scope and limita-	C	Р	08
	tions of a research project			

SYLLABUS MATHEMATICS CORE COURSES

Mathematics Core Courses

Credit, Mark and Hour distribution

Sl. No	Course Code	Course Title	Semester	Total No. of	Contact Hours Hours/week	Credits	Max. Internal Marks	Max. External Marks	Maximum Marks	Exam dur in Hours
1	MTS 1B21	Basic Calculus	1	96	6	4	20	80	100	2.5
2	MTS 2B22	Advanced Calculus	2	96	6	4	20	80	100	2.5
3	MTS 3B23	Abstract Algebra	3	64	4	3	15	60	75	2
4	MTS 3B24	Multivariable Calculus	3	48	3	3	15	60	75	2
5	MTS 4B25	Differential Equations	4	64	4	3	15	60	75	2
6	MTS 4B26	Number Theory	4	48	3	3	15	60	75	2
7	MTS 5B27	Complex Analysis	5	80	5	5	20	80	100	2.5
8	MTS 5B28	Real Analysis - I	5	64	4	4	20	80	100	2.5
9	MTS 6B29	Linear Algebra	6	80	5	4	20	80	100	2.5
10	MTS 6B30	Real Analysis - II	6	64	4	3	15	60	75	2
11	MTS 6B31(E01) MTS 6B31(E02) MTS 6B31(E03)	Elective* Numerical Analysis Introduction to Geometry Linear Programming	6	48	3	3	15	60	75	2
	Total					39				

^{*}One of the following three courses can be offered in the sixth semester as an elective course (Code MTS 6B25(E01), MTS 6B25(E02) and MTS 6B25(E03))

Programme Outcomes

The programme outcomes of the B.Sc Mathematics and Physics (Dual Core) undergraduate programme are the summation of expected course learning outcomes. The possible outcomes of studying Mathematics core courses, are given below:

PO1 Disciplinary knowledge:

Capability of demonstrating comprehensive knowledge of mathematics and understanding of one or more disciplines which form a part of an undergraduate programme of study.

PO2 Communications skills:

- (i) Ability to communicate various concepts of mathematics effectively using examples and their geometrical visualizations.
- (ii) Ability to use mathematics as a precise language of communication in other branches of human knowledge.
- (iii) Ability to show the importance of mathematics as precursor to various scientific developments since the beginning of the civilization.

PO3 Critical thinking:

Ability to employ critical thinking in understanding the concepts in every area of mathematics.

PO4 Analytical reasoning:

Ability to analyze the results and apply them in various problems appearing in different branches of mathematics.

PO5 Problem solving:

- (i) Capability to solve problems using concepts of linear algebra.
- (ii) Capability to solve various models such as growth and decay models, radioactive decay model, LCR circuits and population models using techniques of differential equations.
- (iii) Ability to solve linear system of equations, linear programming problems and network flow problems.
- (iv) Ability to provide new solutions using the domain knowledge of mathematics acquired during this programme.

PO6 Research-related skills:

(i) Capability for inquiring about appropriate questions relating to the concepts in various fields of mathematics.

(ii) To know about the advances in various branches of mathematics.

PO7 Information/digital literacy: Capability to use appropriate software to solve system of equations and differential equations.

PO8 Self-directed learning:

Ability to work independently and do in-depth study of various notions of mathematics.

PO9 Lifelong learning:

Ability to think, acquire knowledge and skills through logical reasoning and to inculcate the habit of self-learning.

PO10 Application skills:

Ability to apply the acquired knowledge in all aspects.

PO11 Experimental skills:

PO12 Moral and ethical awareness/reasoning:

Ability to identify unethical behaviour such as fabrication, falsification ormisrepresentation of data and adopting objective, unbiased and truthful actions in all aspects

Course learning outcomes

Course learning outcomes of each course in B.Sc. Mathematics and Physics Dual Core programme have been enshrined in the beginning of the course contents of each course.

MATHEMATICS CORE COURSES													
Programme	Compulsory										Elective		
outcomes	Basic Calculus	Advanced Calculus	Abstract Algebra	Multivariable Calculus	Differential Equations	Number Theory	Complex Analysis	Real Analysis – I	Linear Algebra	Real Analysis – II	Numerical Analysis	Introduction to Geometry	Linear Programming
Disciplinary knowledge	√	√	✓	√	√	√	√	√	√	✓	√	√	✓
Communication skills	√	✓	√	✓	√	✓	√	✓	✓	√	✓	√	✓
Critical thinking	√	√	✓	✓	√	√	✓	✓	✓	✓	✓	√	✓
Analytical thinking	✓	√	✓			✓				✓	√	✓	
Problem solving	√	√	✓	√	√	√	✓	✓	✓	√	√	√	✓
Research related skills	√		√	√			√		√	√	√		✓
Information/ Digital Literacy	\	✓	✓	✓	✓	✓	✓	√	✓	✓	√	√	✓
Self-directed learning	\	✓	✓	✓	✓	✓	✓	✓	✓	✓	√	✓	✓
Lifelong learning	√			√		✓				✓			
Applicational skills	√	√	✓	√	√	√	√	√	√	✓	√	√	√
Experimental learning	√	√	✓				√	√					✓
Employability options	√			√			√	√				√	√
Ethics	✓	√	✓	√	√	√	✓	✓	√	✓	√	√	√

SEMESTER - I

MTS 1B21: BASIC CALCULUS

6 Hours/Week

4 Credits 100 Marks[Int: 20 + Ext: 80]

Aims, Objectives and Outcomes

The mathematics required for viewing and analyzing the physical world around us is contained in calculus. While Algebra and Geometry provide us very useful tools for expressing the relationship between static quantities, the concepts necessary to explore the relationship between moving/changing objects are provided in calculus. The objective of the course is to introduce students to the fundamental ideas of limit, continuity and differentiability and also to some basic theorems of differential calculus. It is also shown how these ideas can be applied in the problem of sketching of curves and in the solution of some optimization problems of interest in real life. This is done in the first two modules.

The next two modules deal with the other branch of calculus viz. integral calculus. Historically, it is motivated by the geometric problem of finding out the area of a planar region. The idea of definite integral is defined with the notion of limit. A major result is the Fundamental Theorem of Calculus, which not only gives a practical way of evaluating the definite integral but establishes the close connection between the two branches of Calculus. The notion of definite integral not only solves the area problem but is useful in finding out the arc length of a plane curve, volume and surface areas of solids and so on. The integral turns out to be a powerful tool in solving problems in physics, chemistry, biology, engineering, economics and other fields. Some of the applications are included in the syllabus.

Using the idea of definite integral developed, the natural logarithm function is defined and its properties are examined. This allows us to define its inverse function namely the natural exponential function and also the general exponential function. Exponential functions model a wide variety of phenomenon of interest in science, engineering, mathematics and economics. They arise naturally when we model the growth of a biological population, the spread of a disease, the radioactive decay of atoms, and the study of heat transfer problems and so on. We also consider certain combinations of exponential functions namely hyperbolic functions that also arise very frequently in applications such as the study of shapes of cables hanging under their own weight.

Syllabus

Text | Calculus: Soo T Tan Brooks/Cole, Cengage Learning(2010) ISBN: 978-0-534-46579-7

Module - I (24 hrs)

(Functions and Limits)

- 0.2: Functions and their Graphs Definition of a Function, Describing Functions, Evaluating Functions, Finding the Domain of a Function, The Vertical Line Test, Piecewise Defined Functions, Even and Odd Functions (quick review)
- 0.4: Combining functions Arithmetic Operations on Functions, Composition of Functions, Graphs of
 Transformed Functions, Vertical Translations, Horizontal Translations, Vertical
 Stretching and Compressing, Horizontal Stretching and Compressing, Reflecting
- 1.1 : Intuitive introduction to Limits A Real Life Example, Intuitive Definition of a Limit, One-Sided Limits, Using Graphing Utilities to Evaluate Limits
- 1.2: Techniques for finding Limits Computing Limits Using the Laws of Limits, Limits of Polynomial and Rational Functions, Limits of Trigonometric Functions, The Squeeze Theorem.
- 1.3 : Precise Definition of a Limit $\epsilon \delta$ definition. A Geometric Interpretation, Some illustrative examples.
- 1.4: Continuous Functions Continuity at a Number, Continuity at an Endpoint, Continuity on an Interval, Continuity of Composite Functions, Intermediate Value Theorem.
- 1.5: Tangent Lines and Rate of change An Intuitive Look, Estimating the Rate of Change of a Function from its Graph, More Examples Involving Rates of Change, Defining a Tangent Line, Tangent Lines, Secant Lines, and Rates of Change
- 2.1: The Derivatives Definition, Using the Derivative to Describe the Motion of the Maglev, Differentiation, Using the Graph of f to Sketch the Graph of f' Differentiability, Differentiability and Continuity.
- 2.4: The role of derivative in the real world Motion Along a Line, Marginal Functions in Economics
- 2.9 : Differentials and Linear Approximations increments, Differentials, Error Estimates, Linear Approximations, Error in Approximating Δy by dy.

Module - II (24 hrs)

(Applications of the Derivative)

3.1 : Extrema of Functions - Absolute Extrema of Functions, Relative Extrema of Functions, Fermat's Theorem, Finding the Extreme Values of a Continuous Function on a Closed Interval, An Optimization

Problem

- 3.2 : The Mean Value Theorem Rolle's Theorem, The Mean Value Theorem, Some Consequences of the Mean Value Theorem, Determining the number of zeros of a function.
- 3.3: Increasing and Decreasing Functions definition, inferring the behaviour of function from sign of derivative, Finding the relative extrema of a Function, first derivative test
- 3.4: Concavity and Inflection points Concavity, Inflection Points, The Second Derivative Test, The Roles of f' and f'' in Determining the Shape of a Graph
- 3.5 : Limits involving Infinity; Asymptotes Infinite Limits, Vertical Asymptotes, Limits at Infinity, Horizontal Asymptotes, Infinite Limits at Infinity, Precise Definitions
- 3.6 : Curve Sketching The Graph of a Function, Guide to Curve Sketching, Slant Asymptotes, Finding Relative Extrema Using a Graphing Utility
- 3.7 : Optimization Problems guidelines for finding absolute extrema, Formulating Optimization Problems- application involving several real life problems
- (Integration) 4.1: Anti derivatives, Indefinite integrals, Basic Rules of Integration, a few basic integration formulas and rules of integration, Differential Equations, Initial ValueProblems
- 4.3: Area An Intuitive Look, The Area Problem, Defining the Area of the Region Under the Graph of a Function-technique of approximation ['Sigma Notation' and 'Summation Formulas' Omitted] An Intuitive Look at Area (Continued), Defining the Area of the Region Under the Graph of a Function-precise definition, Area and Distance

Module - III (24 hrs)

- 4.4: The Definite Integral Definition of the Definite Integral, Geometric Interpretation of the Definite Integral, The Definite Integral and Displacement, Properties of the Definite Integral, More General Definition of the Definite Integral
- 4.5 : The Fundamental Theorem of Calculus How Are Differentiation and Integration Related?, The Mean Value Theorem for Definite Integrals, The Fundamental Theorem of Calculus: Part I, inverse relationship between differentiation and integration, Fundamental Theorem of Calculus: Part 2, Evaluating Definite Integrals Using Substitution, Definite Integrals of Odd and Even Functions, The Definite Integral as a Measure of Net Change

(Applications of Definite Integral)

5.1: Areas between Curves - A Real Life Interpretation, The Area Between Two Curves, Integrating with Respect to y-adapting to the shape of the region, What happens when the Curves Intertwine?

- 5.2: Volume Solids of revolution, Volume by Disk Method, Region revolved about the x-axis, Region revolved about the y-axis, Volume by the Method of Cross Sections ['Washer Method'omitted]
- 5.4: Arc Length and Areas of surfaces of revolution- Definition of Arc Length, Length of a Smooth Curve, arc length formula, The Arc Length Function, arc length differentials, Surfaces of Revolution, surface area as surface of revolution,
- 5.5: Work-Work Done by a Constant Force, Work Done by a Variable Force, Hook's Law, Moving non rigid matter, Work done by an expanding gas 5.7: Moments and Center of Mass Measures of Mass, Center of Mass of a System on a Line, Center of Mass of a System in the Plane, Center of Mass of Laminas [upto and including Example 3; rest of the section omitted]

$$Module - IV$$
 (24 hrs)

(The Transcendental Functions)

- 6.1: The Natural logarithmic function definition, The Derivative of $\ln x$, Laws of Logarithms, The Graph of the Natural Logarithmic Function, The Derivatives of Logarithmic Functions, Logarithmic Differentiation, Integration Involving Logarithmic Functions
- 6.2: Inverse Functions The Inverse of a Function, The Graphs of Inverse Functions, Which Functions have Inverses?, Finding the Inverse of a Function, Continuity and Differentiability of Inverse Functions.
- 6.3: Exponential Functions The number e, Defining the Natural Exponential Function, properties, The Laws of Exponents, The Derivatives of Exponential Functions, Integration of the Natural Exponential Function
- 6.4: General Exponential and Logarithmic Functions Exponential Functions with Base a, laws of exponents, The Derivatives of a^x , a^u , Graphs of $y = a^x$, integrating a^x , Logarithmic Functions with Base a, change of base formula, The Power Rule (General Form), The Derivatives of Logarithmic Functions with Base a, The Definition of the Number e as a Limit ['Compound Interest' omitted]
- 6.5: Inverse trigonometric functions definition, graph, inverse properties, Derivative of inverse trigonometric functions, Integration Involving Inverse Trigonometric Functions
- 6.6: Hyperbolic functions The Graphs of the Hyperbolic Functions, Hyperbolic Identities, Derivatives and Integrals of Hyperbolic Functions, Inverse Hyperbolic Functions, representation in terms of logarithmic function, Derivatives of Inverse Hyperbolic Functions, An Application
- 6.7: Indeterminate forms and L Hospital's rule-motivation, The Indeterminate forms $\frac{0}{0}$ and $\frac{\infty}{\infty}$, The Indeterminate forms $\infty \infty$ and $0 \cdot \infty$. The Indeterminate forms 0^0 , ∞^0 and 1^∞
- 7.6: Improper integrals definition, Infinite Intervals of Integration, Improper Integrals with Infinite Discontinuities, A Comparison Test for Improper Integrals

References:

- 1. Joel Hass, Christopher Heil & Maurice D. Weir: Thomas' Calculus (14/e), Pearson (2018) ISBN: 0134438981
- 2. Robert A Adams & Christopher Essex : Calculus Single Variable (8/e) Pearson Education Canada (2013) ISBN: 0321877403
- 3. Jon Rogawski & Colin Adams : Calculus Early Transcendentals (3/e) W. H. Freeman and Company (2015) ISBN: 1319116450
- 4. Anton, Bivens & Davis : Calculus Early Transcendentals (11/e) John Wiley & Sons, Inc.(2016) ISBN: 1118883764
- 5. James Stewart : Calculus (8/e) Brooks/Cole Cengage Learning(2016) ISBN: 978-1-285-74062-1
- 6. Jerrold Marsden & Alan Weinstein : Calculus I and II (2/e) Springer Verlag NY (1985) ISBN:0-387-90974-5, ISBN: 0-387-90975-3

SEMESTER - II

MTS 2B22: ADVANCED CALCULUS

6 Hours/Week

4 Credits 100 Marks[Int: 20 + Ext : 80]

Aims, Objectives and Outcomes

After this course, the students are introduced to the idea of improper integrals, their convergence and evaluation. This enables to study a related notion of convergence of a series, which is practically done by applying several different tests such as integral test, comparison test and so on. As a special case, a study on power series- their region of convergence, differentiation and integration etc.,- is also done.

A detailed study of plane and space curves is then taken up. The students get the idea of parametrization of curves, they learn how to calculate the arc length, curvature etc. using parametrization and also the area of surface of revolution of a parametrized plane curve. Students are introduced into other coordinate systems which often simplify the equation of curves and surfaces and the relationship between various coordinate systems are also taught. This enables them to directly calculate the arc length and surface areas of revolution of a curve whose equation is in polar form.

In the first two modules of this course, the students will be able to handle vectors in dealing with the problems involving geometry of lines, curves, planes and surfaces in space and have acquired the ability to sketch curves in plane and space given in vector valued form.

The next module useful ideas and notions such as limit, continuity, derivative and integral seen in the context of function of single variable to function of several variables. The corresponding results will be the higher dimensional analogues of what we learned in the case of single variable functions.

The successful completion of the course will enable the student to

- Understand several contexts of appearance of multivariable functions and their representation using graph and contour diagrams.
- Formulate and work on the idea of limit and continuity for functions of several variables.
- Understand the notion of partial derivative, their computation and interpretation.
- Understand chain rule for calculating partial derivatives.
- Get the idea of directional derivative, its evaluation, interpretation, and relationship with partial derivatives.
- Understand the concept of gradient, a few of its properties, application and interpretation.
- Understand the use of partial derivatives in getting information of tangent plane and normal line.

- Calculate the maximum and minimum values of a multivariable function using second derivative test and Lagrange multiplier method.
- Find a few real life applications of Lagrange multiplier method in optimization problems.

Syllabus

Calculus: Soo T Tan Brooks/Cole, Cengage Learning(2010) ISBN: 978-0-534-46579-7

Module - I(24 hrs)

(Infinite Sequences and Series)

Text

- Sequences definition, recursive definition, Limit of a Sequence, limit laws, squeeze theorem, Bounded Monotonic Sequences, definition, monotone convergence theorem (only statement; its proof omitted)
- 9.2: Series defining the sum, convergence and divergence, Geometric Series, The Harmonic Series, The Divergence Test, Properties of Convergent Series
- 9.3: The Integral Test investigation of convergence, integral test, The p series, its convergence and divergence
- 9.4: The Comparison Test test series, The Comparison Test, The Limit Comparison Test
- 9.5: Alternating Series definition, the alternating series test, its proof, examples, Approximating the Sum of an Alternating Series by S_n
- 9.6: Absolute Convergence definition, conditionally convergent, The Ratio Test, The Root Test, Summary of Tests for Convergence and Divergence of Series, Rearrangement of Series
- 9.7: Power Series definition, Interval of Convergence, radius of convergence, Differentiation and Integration of Power Series
- Taylor and Maclaurin Series definition, Taylor and Maclaurin series of functions, Techniques for Finding Taylor Series

Module – II (24 hrs)

- 10.2: Plane Curves and Parametric Equations Why we use Parametric Equations, Sketching Curves Defined by Parametric Equations
- 10.3: The Calculus of parametric equations Tangent Lines to Curves Defined by Parametric Equations, Horizontal and Vertical Tangents, Finding $\frac{d^2y}{dx^2}$ from Parametric Equations, The Length of a Smooth Curve, The Area of a Surface of Revolution

- 10.4 : Polar coordinate The Polar Coordinate System, Relationship Between Polar and Rectangular Coordinates, Graphs of Polar Equations, Symmetry, Tangent Lines to Graphs of Polar Equations
- 10.5: Areas and Arc Lengths in polar coordinates Areas in Polar Coordinates, area bounded by polar curves, Area Bounded by Two Graphs, Arc Length in Polar Coordinates, Area of a Surface of Revolution, Points of Intersection of Graphs in Polar Coordinates
- 11.5: Lines and Planes in Space Equations of Lines in Space, parametric equation, symmetric equation of a line, Equations of Planes in Space, standard equation, Parallel and Orthogonal Planes, The Angle Between Two Planes, The Distance Between a Point and a Plane
- 11.6: Surfaces in Space Traces, Cylinders, Quadric Surfaces, Ellipsoids, Hyperboloids of One Sheet, Hyperboloids of Two Sheets, Cones, Paraboloids, Hyperbolic Paraboloids
- 11.7: Cylindrical and Spherical Coordinates The Cylindrical Coordinate System, converting cylindrical to rectangular and vice verse, The Spherical Coordinate System, converting spherical to rectangular and vice verse,

Module - III (24 hrs)

- 12.1 : Vector Valued functions and Space Curves definition of vector function, Curves Defined by Vector Functions, ['Example 7' omitted] Limits and Continuity
- 12.2 : Differentiation and Integration of Vector Valued Function The Derivative of a Vector Function, Higher Order Derivatives, Rules of Differentiation, Integration of Vector Functions
- 12.3: Arc length and Curvature Arc Length of a space curve, Smooth Curves, Arc Length Parameter, arc length function, Curvature, formula for finding curvature, Radius of Curvature.
- 12.4: Velocity and Acceleration Velocity, Acceleration, and Speed; Motion of a Projectile
- 12.5: Tangential and Normal Components of Acceleration The Unit Normal, principal unit normal vector, Tangential and Normal Components of Acceleration [The subsections Kepler's Laws of Planetary Motion, and Derivation of Kepler's First Law omitted]
- 13.1 : Functions of two or more variables Functions of Two Variables, Graphs of Functions of Two Variables, Level Curves, Functions of Three Variables and Level Surfaces
- 13.2 : Limits and continuity An Intuitive Definition of a Limit, existence and non existence of limit, Continuity of a Function of Two Variables, Continuity on a Set, continuity of polynomial and rational functions, continuity of composite functions, Functions of Three or More Variables, The $\epsilon-\delta$ Definition of a Limit
- 13.3 : Partial Derivatives Partial Derivatives of Functions of Two Variables, geometric interpretation, Computing Partial Derivatives, Implicit Differentiation, Partial Derivatives of Functions of More Than

Two Variables, Higher Order Derivatives, clairaut theorem, harmonic functions

Module - IV (24 hrs)

- 13.4 : Differentials Increments, The Total Differential, interpretation, Error in Approximating Δz by dz [only statement of theorem1 required; proof omitted] Differentiability of a Function of Two Variables, criteria, Differentiability and Continuity, Functions of Three or More Variables
- 13.5: The Chain rule The Chain Rule for Functions Involving One Independent Variable, The Chain Rule for Functions Involving Two Independent Variables, The General Chain Rule, Implicit Differentiation
- 13.6: Directional Derivatives and Gradient vectors The Directional Derivative, The Gradient of a Function of Two Variables, Properties of the Gradient, Functions of Three Variables
- 13.7: Tangent Planes and Normal Lines Geometric Interpretation of the Gradient, Tangent Planes and Normal Lines, Using the Tangent Plane of f to approximate the Surface z = f(x, y)
- 13.8 : Extrema of Functions of two variables Relative and Absolute Extrema, Critical Points Candidates for Relative Extrema, The Second Derivative Test for Relative Extrema, Finding the Absolute Extremum Values of a Continuous Function on a Closed Set
- 13.9: Lagrange Multipliers Constrained Maxima and Minima, The Method of Lagrange Multipliers, Lagrange theorem, Optimizing a Function Subject to Two Constraints

References:

- 1. Joel Hass, Christopher Heil & Maurice D. Weir : Thomas' Calculus (14/e), Pearson (2018) ISBN: 0134438981
- 2. Robert A Adams & Christopher Essex : Calculus Single Variable (8/e) Pearson Education Canada (2013) ISBN: 0321877403
- 3. Jon Rogawski & Colin Adams : Calculus Early Transcendentals (3/e) W. H. Freeman and Company (2015) ISBN: 1319116450
- 4. Anton, Bivens & Davis : Calculus Early Transcendentals (11/e) John Wiley & Sons, Inc.(2016) ISBN: 1118883764
- 5. James Stewart: Calculus (8/e) Brooks/Cole Cengage Learning(2016) ISBN: 978-1-285-74062-1
- Jerrold Marsden & Alan Weinstein: Calculus I and II (2/e) Springer Verlag NY (1985) ISBN:0-387-90974-5, ISBN: 0-387-90975-3

SEMESTER - III

MTS 3B23: ABSTRACT ALGEBRA

4 Hours/Week

3 Credits 75 Marks[Int: 15 + Ext: 60]

Aims, Objectives and Outcomes

The brilliant mathematician Evariste Galois developed an entire theory that connected the solvability by radicals of a polynomial equation with the permutation group of its roots. The theory now known as Galois theory solves the famous problem of insolvability of quintic. A study on symmetric functions now becomes inevitable. One can now observe the connection emerging between classical algebra and modern algebra. The last three modules are therefore devoted to the discussion on basic ideas and results of abstract algebra. Students understand the abstract notion of a group, learn several examples, are taught to check whether an algebraic system forms a group or not and are introduced to some fundamental results of group theory. The idea of structural similarity, the notion of cyclic group, permutation group, various examples and very fundamental results in the areas are also explored.

Syllabus

Text:	Abstract Algebra (3/e): John A Beachy and William D Blair Waveland Press, Inc.(2006),
	ISBN: 1-57766-443-4

Module - I (16 hrs)

(The Transcendental Functions)

- 1.4: Integers modulo n congruence class modulo n, addition and multiplication, divisor of zero, multiplicative inverse
- 2.2 : Equivalence relations basic idea, definition, equivalence class, factor set, partition and equivalence relation, examples and illustrations
- 2.3 : Permutations definition, cycles, product of cycles, permutation as product of disjoint cycles, order of cycles, transposition, even and odd transpositions

Module - II (16 hrs)

- 3.1: Definition of Group binary operation, uniqueness of identity and inverse, definition and examples of groups, properties, Abelian group, finite and infinite groups, general linear groups
- 3.2 : Subgroups the notion of subgroup, examples, conditions for a subgroup, cyclic subgroups, order of an element, Lagrange theorem, Euler's theorem

- 3.3 : Constructing examples groups with order upto 6, multiplication table, product of subgroups, direct products, Klein four group as direct product, subgroup generated by a subset
- 3.4 : Isomorphism definition, consequences, structural properties, method of showing that groups are not isomorphic, isomorphic and non isomorphic groups.

Module - III (16 hrs)

- 3.5 : Cyclic groups subgroups of cyclic groups, characterisation, generators of a finite cyclic group, structure theorem for finite cyclic group, exponent of a group, characterisation of cyclic groups among finite abelian groups.
- 3.6: Permutation groups definition, Cayley's theorem, rigid motions of n-gons, dihedral group, alternating group
- 3.7 : Homomorphism basic idea, examples, definition, properties, kernel, normal subgroups, subgroups related via homomorphism
- 3.8 : Cosets left and right cosets, normal subgroups and factor groups, fundamental homomorphism theorem, simple groups, examples and illustrations of concepts

Module - IV (16 hrs)

- 7.1 : (Structure of Groups) Isomorphism theorems; Automorphism first isomorphism theorem, second isomorphism theorem, inner automorphism
- 5.1 : Commutative Rings; Integral Domains definition, examples, subring, criteria to be a subring, divisor of zero, integral domain, finite integral domain.

- 1. Joseph A. Gallian : Contemporary Abstract Algebra (9/e), Cengage Learning, Boston (2017), ISBN: 978-1-305-65796-0
- 2. John B Fraleigh: A First Course in Abstract Algebra (7/e) Pearson Education LPE (2003) ISBN 978-81-7758-900-9
- 3. David Steven Dummit, Richard M. Foote: Abstract Algebra (3/e), Wiley, (2004), ISBN: 8126532289
- 4. Linda Gilbert and Jimmie Gilbert: Elements of Modern Algebra (8/e), Cengage Learning, Stamford (2015), ISBN: 1-285-46323-4
- 5. John R. Durbin: Modern Algebra: An Introduction (6/e), Wiley (2015), ISBN: 1118117611
- Jeffrey Bergen: A Concrete Approach to Abstract Algebra From the integers to Insolvability of Quintic, Academic Pres [Elsever] (2010), ISBN: 978-0-12-374941-3

SEMESTER - III

MTS 3B24: MULTIVARIABLE CALCULUS

3 Hours/Week

3 Credits 75 Marks[Int: 15 + Ext: 60]

Aims, Objectives and Outcomes

The intention of the course is to extend the immensely useful ideas and notions such as limit, continuity, derivative and integral seen in the context of function of single variable to function of several variables. The corresponding results will be the higher dimensional analogues of what we learned in the case of single variable functions. The results we develop in the course of calculus of multivariable is extremely useful in several areas of science and technology as many functions that arise in real life situations are functions of multivariable.

The successful completion of the course will enable the student to

- Extend the notion of integral of a function of single variable to integral of functions of two and three variables.
- Address the practical problem of evaluation of double and triple integral using Fubini's theorem and change of variable formula.
- Realise the advantage of choosing other coordinate systems such as polar, spherical, cylindrical etc. in the evaluation of double and triple integrals.
- See a few applications of double and triple integral in the problem of finding out surface area, mass of lamina, volume, centre of mass and soon.
- Understand the notion of a vector field, the idea of curl and divergence of a vector field, their evaluation and interpretation.
- Understand the idea of line integral and surface integral and their evaluations.
- Learn three major results viz. Green's theorem, Gauss's theorem and Stokes' theorem of multivariable calculus and their use in several areas and directions.

Text | Calculus: Soo T Tan Brooks/Cole, Cengage Learning (2010) ISBN: 978-0-534-46579-7

Module - I (16 hrs)

- 14.1 :Double integrals An Introductory Example, Volume of a Solid Between a Surface and a Rectangle, The Double Integral Over a Rectangular Region, Double Integrals Over General Regions, Properties of Double Integrals
- 14.2 : Iterated Integrals Iterated Integrals Over Rectangular Regions, Fubini's Theorem for Rectangular Regions, Iterated Integrals Over Non rectangular Regions, y-simple and x- simple regions, advantage of changing the order of integration
- 14.3: Double integrals in polar coordinates Polar Rectangles, Double Integrals Over Polar Rectangles, Double Integrals Over General Regions, r- simple region, method of evaluation
- 14.4 : Applications of Double integral Mass of a Lamina, Moments and Center of Mass of a Lamina, Moments of Inertia, Radius of Gyration of a Lamina
- 14.5 : Surface Area of a Surface z = f(x, y), Area of Surfaces with Equations y = g(x, z) and x = h(y, z)

Module - II (16 hrs)

- 14.6: Triple integrals Triple Integrals Over a Rectangular Box, definition, method of evaluation as iterated integrals, Triple Integrals Over General Bounded Regions in Space, Evaluating Triple Integrals Over General Regions, evaluation technique, Volume, Mass, Center of Mass, and Moments of Inertia
- 14.7: Triple Integrals in cylindrical and spherical coordinates evaluation of integrals in Cylindrical Coordinates, Spherical Coordinates
- 14.8 : Change of variables in multiple integrals Transformations, Change of Variables in Double Integrals [only the method is required; derivation omitted], illustrations, Change of Variables in Triple Integrals
- 15.2: Vector Fields V.F. in two and three dimensional space, Conservative Vector Fields
- 15.3: Divergence and Curl- Divergence- idea and definition, Curl idea and definition
- 15.4: Line Integrals Line integral w.r.t. arc length-motivation, basic idea and definition, Line Integrals with Respect to Coordinate Variables, orientation of curve Line Integrals in Space, Line Integrals of Vector Fields
- 15.5: Independence of Path and Conservative Vector Fields path independence through example, definition, fundamental theorem for line integral, Line Integrals Along Closed Paths, work done by conservative vector field, Independence of Path and Conservative Vector Fields, Determining Whether

a Vector Field is Conservative, test for conservative vector field Finding a Potential Function, Conservation of Energy

Module - III (16 hrs)

- 15.6: Green's Theorem Green's Theorem for Simple Regions, proof of theorem for simple regions, finding area using line integral, Green's Theorem for More General Regions, Vector Form of Green's Theorem
- 15.7: Parametric Surfaces Why We Use Parametric Surfaces, Finding Parametric Representations of Surfaces, Tangent Planes to Parametric Surfaces, Area of a Parametric Surface [derivation of formula omitted]
- 15.8: Surface Integrals Surface Integrals of Scalar Fields, evaluation of surface integral for surfaces that are graphs, [derivation of formula omitted; only method required] Parametric Surfaces, evaluation of surface integral for parametric surface, Oriented Surfaces, Surface Integrals of Vector Fields definition, flux integral, evaluation of surface integral for graph[method only], Parametric Surfaces, evaluation of surface integral of a vector field for parametric surface [method only]
- 15.9: The Divergence Theorem divergence theorem for simple solid regions (statement only), illustrations, Interpretation of Divergence
- 15.10 : Stokes Theorem generalization of Green's theorem -Stokes Theorem, illustrations, Interpretation of Curl

- 1. Joel Hass, Christopher Heil & Maurice D. Weir: Thomas' Calculus (14/e), Pearson (2018), ISBN: 0134438981
- 2. Robert A Adams & Christopher Essex : Calculus Single Variable (8/e), Pearson Education Canada (2013) ISBN: 0321877403
- 3. Jon Rogawski & Colin Adams : Calculus Early Transcendentals (3/e), W. H. Freeman and Company (2015), ISBN: 1319116450
- 4. Anton, Bivens & Davis: Calculus Early Transcendentals (11/e), John Wiley & Sons, Inc. (2016), ISBN: 1118883764
- 5. James Stewart: Calculus (8/e) Brooks/Cole Cengage Learning(2016) ISBN: 978-1-285-74062-1
- Jerrold Marsden & Alan Weinstein : Calculus I and II (2/e), Springer Verlag NY (1985), ISBN:0-387-90974-5, ISBN: 0-387-90975-3
- Arnold Ostebee & Paul Zorn: Multivariable Calculus (2/e), W. H. Freeman Custom Publishing, N.Y.(2008)ISBN: 978-1-4292-3033-9

SEMESTER - IV

MTS 4B25: DIFFERENTIAL EQUATIONS

4 Hours/Week

3 Credits 75 Marks[Int: 15 + Ext: 60]

Aims, Objectives and Outcomes

Differential equations model the physical world around us. Many of the laws or principles governing natural phenomenon are statements or relations involving rate at which one quantity changes with respect to another. The mathematical formulation of such relations (modelling) often results in an equation involving derivative (differential equations). The course is intended to find out ways and means for solving differential equations and the topic has wide range of applications in physics, chemistry, biology, medicine, economics and engineering. On successful completion of the course, the students shall acquire the following skills/knowledge.

- Students could identify a number of areas where the modelling process results in a differential equation.
- They will learn what an ODE is, what it means by its solution, how to classify DEs, what it means by an IVP and so on.
- They will learn to solve DEs that are in linear, separable and in exact forms and also to analyse the solution.
- They will realise the basic differences between linear and non linear DEs and also basic results that guarantees a solution in each case.
- They will learn a method to approximate the solution successively of a first order IVP.
- They will become familiar with the theory and method of solving a second order linear homogeneous and nonhomogeneous equation with constant coefficients.
- They will learn to find out a series solution for homogeneous equations with variable coefficients near ordinary points.
- Students acquire the knowledge of solving a differential equation using Laplace method which is especially suitable to deal with problems arising in engineering field.

Text : Elementary Differential Equations and Boundary Value Problems (11/e): William E Boyce, Richard C Diprima and Douglas B Meade John Wiley & Sons (2017), ISBN : 1119169879

Module - I (16 hrs)

- 1.1 : Some Basic Mathematical Models; Direction Fields
- 1.2 : Solutions of some Differential equations
- 1.3 : Classification of Differential Equations
- 2.1: Linear Differential Equations; Method of Integrating Factors
- 2.2: Separable Differential Equations
- 2.3: Modelling with First Order Differential Equations
- 2.4: Differences Between Linear and Nonlinear Differential Equations

Module - II (16 hrs)

- 2.6 : Exact Differential Equations and Integrating Factors
- 2.8: The Existence and Uniqueness Theorem (proof omitted)
- 3.1: Homogeneous Differential Equations with Constant Coefficients
- 3.2 : Solutions of Linear Homogeneous Equations; the Wronskian
- 3.3 : Complex Roots of the Characteristic Equation

Module – III (16 hrs)

- 3.4: Repeated Roots; Reduction of Order
- 3.5: Nonhomogeneous Equations; Method of Undetermined Coefficients
- 3.6 : Variation of Parameters
- 5.2 : Series solution near an ordinary point, part1
- 5.3: Series solution near an ordinary point, part2

Module - IV (16 hrs)

6.1 : Definition of the Laplace Transform

6.2 : Solution of Initial Value Problems

6.3: Step Functions

6.5: Impulse Functions

6.6: The Convolution Integral

- 1. Dennis G Zill & Michael R Cullen: Differential Equations with Boundary Value Problems (7/e): Brooks/Cole Cengage Learning (2009), ISBN: 0495108367
- 2. R Kent Nagle, Edward B. Saff & Arthur David Snider: Fundamentals of Differential Equations (8/e) Addison Wesley (2012) ISBN: 0321747739
- 3. C. Henry Edwards & David E. Penney: Elementary Differential Equations (6/e) Pearson Education, Inc. New Jersey (2008), ISBN 0132397307
- 4. John Polking, Albert Boggess & David Arnold: Differential Equations with Boundary Value Problems (2/e) Pearson Education, Inc New Jersey (2006) ISBN 0131862367
- 5. Henry J. Ricardo: A Modern Introduction to Differential Equations (2/e) Elsevier Academic Press. (2009). ISBN: 9780123747464
- James C Robinson: An Introduction to Ordinary Differential Equations Cambridge University Press (2004). ISBN: 0521533910

SEMESTER - IV

MTS 4B26: NUMBER THEORY

3 Hours/Week

3 Credits 75 Marks[Int: 15 + Ext: 60]

Aims, Objectives and Outcomes

The classical number theory is introduced and some of the very fundamental results are discussed in other modules. It is hoped that the method of writing a formal proof, using proof methods discussed in the first module, is best taught in a concrete setting, rather than as an abstract exercise in logic. Number theory, unlike other topics such as geometry and analysis, does not suffer from too much abstraction and the consequent difficulty in conceptual understanding. Hence, it is an ideal topic for a beginner to illustrate how mathematicians do their normal business. By the end of the course, the students will be able to enjoy and master several techniques of problem solving such as recursion, induction etc., the importance of pattern recognition in mathematics, the art of conjecturing and a few applications of number theory. Enthusiastic students will have acquired knowledge to read and enjoy on their own a few applications of number theory in the field of art, geometry and coding theory.

Successful completion of the course enables students to

The successful completion of the course will enable the student to

- Prove results involving divisibility, greatest common common divisor, least common multiple and a few applications.
- Understand the theory and method of solutions of LDE.
- Solve linear congruent equations.
- Learn three classical theorems viz. Wilson's theorem, Fermat's little theorem and Euler's theorem and a few important consequences.

Text | Elementary Number Theory with Applications (2/e): Thomas Koshy, Elsever Academic Press (2007), ISBN: 978-0-12-372487-8

Module - I (16 hrs)

- 1.3: Mathematical induction- well ordering principle, simple applications, weak version of principle of mathematical induction, illustrations, strong version of induction (second principle of MI), illustration
- 1.4: Recursion- recursive definition of a function, illustrations.
- 2.1: The division algorithm statement and proof, div & mod operator, card dealing, The two queens puzzle (simple applications), pigeonhole principle and division algorithm, divisibility relation, illustration, divisibility properties, union intersection and complement-inclusion exclusion principle & applications, even and odd integers.
- 2.5: Prime and Composite Numbers definitions, infinitude of primes, ['algorithm 2.4' omitted]. The sieve of Eratosthenes, a number theoretic function, prime number theorem (statement only), distribution of primes (upto and including Example 2.25). [rest of the section omitted]
- 3.1: Greatest Common Divisor gcd, symbolic definition, relatively prime integers, Duncan's identity, Polya's theorem, infinitude of primes, properties of gcd, linear combination, gcd as linear combination, an alternate definition of gcd, gcd of n positive integers, a linear combination of n positive integers, pairwise relatively prime integers, alternate proof for infinitude of prime.

Module - II (16 hrs)

- 3.2 : The Euclidean Algorithm The Euclidean algorithm [algorithm 3.1 omitted], A jigsaw puzzle, Lame's theorem (statement only; proof omitted)
- 3.3: The Fundamental Theorem of Arithmetic Euclid's lemma on division of product by a prime, fundamental theorem of arithmetic, Canonical Decomposition, number of trailing zeros, highest power of a prime dividing!, [only statement of Theorem3.14 required; proof omitted] Distribution of Primes Revisited, Dirichlet's Theorem (statement only)
- 3.4: Least Common Multiple definition, canonical decomposition to find lcm, relationship between gcd and lcm, relatively prime numbers and their lcm
- 3.5: Linear Diophantine Equations LDE in two variables, conditions to have a solution, Aryabhatta's method, number of solutions, general solution, Mahavira's puzzle, hundred fowls puzzle, Monkey and

Coconuts Puzzle, ['Euler's method for solving LDE's' omitted] Fibonacci numbers and LDE, LDE in more number of variables and their solutions - Theorem 3.20

- 4.1: Congruences congruence modulo m, properties of congruence, characterization of congruence, least residue, ['Friday-the-Thirteenth' omitted], congruence classes, A Complete Set of Residues Modulo m, properties of congruence, use of congruence to find the remainder on division, ['Modular Exponentiation' method omitted], Towers of Powers Modulo m, further properties of congruence and their application to find remainder ['Monkey and Cocunut Puzzle revisited' (example 4.17) omitted] congruences of two numbers with different moduli
- 4.2 : Linear Congruence solvability, uniqueness of solution, incongruent solutions, Modular Inverses, applications

Module - III (16 hrs)

- 5.1: Divisibility Tests-Divisibility Test for 10, Divisibility Test for 5, Divisibility Test for 2, Divisibility Tests for 3 and 9, Divisibility Test for 11 [rest of the section from Theorem 5.1 onwards omitted]
- 7.1 : Wilson's Theorem self invertible modulo prime, Wilson's theorem and its converse ['Factorial, Multifactorial and Primorial Primes' omitted]
- 7.2: Fermat's Little Theorem(FLT)- FLT and its applications, [Lagrange's alternate proof of Wilson's theorem omitted], inverse of a modulo p using FLT, application-solution of linear congruences ['Factors of 2^n+1 ' omitted], extension of FLT in various directions ['The Pollard p-1 factoring method' omitted]
- 7.4 : Euler's Theorem- motivation, Euler's Phi Function ϕ , Euler's Theorem, applications, generalisation of Euler's theorem (koshy)

- 1. David M. Burton: Elementary Number Theory (7/e). McGraw-Hill (2011), ISBN: 978-0-07-338314-9
- 2. Gareth A. Jones and J. Mary Jones: Elementary Number Theory, Springer Undergraduate Mathematics Series (1998), ISBN: 978-3-540-76197-6
- 3. Underwood Dudley: Elementary Number Theory (2/e), Dover Publications (2008), ISBN: 978-0-486-46931-7
- 4. James K Strayer : Elementary Number Theory, Waveland Press, inc. (1994), ISBN:978-1-57766-224-2
- 5. Kenneth H. Rosen: Elementary Number Theory (6/e), Pearson Education (2018), ISBN: 9780134310053

SEMESTER - V

MTS 5B27: COMPLEX ANALYSIS

5 Hours/Week

5 Credits 100 Marks[Int: 20 + Ext: 80]

Aims, Objectives and Outcomes

The course is aimed to provide a thorough understanding of complex function theory. It is intended to develop the topics in a fashion analogous to the calculus of real functions. At the same time differences in both theories are clearly emphasised. When real numbers are replaced by complex numbers in the definition of derivative of a function, the resulting complex differentiable functions (more precisely analytic functions) turn out to have many remarkable properties not possessed by their real analogues. These functions have numerous applications in several areas of mathematics such as differential equations, number theory etc. and also in science and engineering. The focus of the course is on the study of analytic functions and their basic behaviour with respect to the theory of complex calculus.

The course enables students

- to understand the difference between differentiability and analyticity of a complex function and construct examples.
- to understand necessary and sufficient condition for checking analyticity.
- to know of harmonic functions and their connection with analytic functions
- to know a few elementary analytic functions of complex analysis and their properties.
- to understand definition of complex integral, its properties and evaluation.
- to know a few fundamental results on contour integration theory such as Cauchy's theorem, Cauchy-Goursat theorem and their applications.
- to understand and apply Cauchy's integral formula and a few consequences of it such as Liouville's theorem, Morera's theorem and so forth in various situations.
- to see the application of Cauchy's integral formula in the derivation of power series expansion of an analytic function.
- to know a more general type of series expansion analogous to power series expansion viz. Laurent's series expansion for functions having singularity.
- to understand how Laurent's series expansion lead to the concept of residue, which in turn provide another fruitful way to evaluate complex integrals and, in some cases, even real integrals.
- to see another application of residue theory in locating the region of zeros of an analytic function.

Text | Complex Analysis A First Course with Applications (3/e): Dennis Zill & Patric Shanahan, Jones and Bartlett Learning (2015), ISBN: 1-4496-9461-6

Module - I (20 hrs)

Analytic Functions

- 3.1: Limit and Continuity Limit of a complex function, condition for non existence of limit, real and imaginary parts of limit, properties of complex limits, continuity, discontinuity of principal square root function, properties of continuous functions, continuity of polynomial and rational functions, Bounded Functions, Branches, Branch Cuts and Points
- 3.2 : Differentiability and Analyticity Derivative of a complex Function, rules of differentiation, function that is nowhere differentiable, Analytic functions, entire functions, singular points, Analyticity of sum product and quotient, L'Hospital rule
- 3.3 : Cauchy Riemann Equations Necessary condition for analyticity, Criterion for non analyticity, sufficient condition for analyticity, sufficient condition for differentiability, Cauchy Riemann equations in polar coordinates
- 3.4 : Harmonic Functions definition, analyticity and harmonic nature, harmonic conjugate functions, finding harmonic conjugate

Elementary Functions

4.1: Exponential and logarithmic functions-Complex Exponential Function, its derivative, analyticity, modulus argument and conjugate, algebraic properties, periodicity, exponential mapping and its properties, Complex Logarithmic Function, logarithmic identities, principal value of a complex logarithm, Ln z as inverse function, derivative, logarithmic mapping, properties, other branches

$$Module - II$$
 (20 hrs)

4.3: Trigonometric and Hyperbolic functions - Complex Trigonometric Functions, identities, periodicity of sine and cosine, Trigonometric equations and their solution, Modulus, zeros, analyticity, [subsection 'Trigonometric Mapping' omitted], Complex Hyperbolic Functions, relation to sine and cosine

Integration in the Complex plane

- 5.1 : Real Integrals Definite Integral, simple, smooth, closed curves, Line integrals in the plane, Method of Evaluation-curves defined parametrically and curves given as functions, Orientation of a Curve
- 5.2 : Complex Integral contours, definition of complex integral, complex valued function of a real variable, evaluation of contour integral, properties of contour integral, ML-inequality
- 5.3 : Cauchy–Goursat Theorem simply and multiply connected regions, Cauchy theorem, Cauchy–Goursat theorem for simply connected domain (without proof), Multiply Connected Domains, principe of deformation of contours, Cauchy–Goursat theorem for multiply connected domains, illustrations
- 5.4: Independence of Path definition, analyticity and path independence, anti derivative, Fundamental theorem for contour integrals, Some Conclusions, Existence of anti derivative

$$Module - III$$
 (20 hrs)

- 5.5 : Cauchy's Integral Formulas & their Consequences Cauchy's Two Integral Formulas, illustration of their use, Some Consequences of the Integral Formulas cauchy's inequality, Liouville theorem, Morera's theorem, Maximum modulus theorem
- 6.1: Sequences and Series definition, criteria for convergence, Geometric series, necessary condition for convergence, test for divergence, absolute and conditional convergence, Ratio test, root test, Power Series, circle of convergence, radius of convergence, Arithmetic of Power Series
- 6.2 : Taylor Series differentiation and integration of power series, term by term differentiation and integration, Taylor Series, Maclaurian series, illustrations
- 6.3: Laurent's Series isolated singularities, Laurent's Theorem [proof omitted], illustrations

$$Module - IV$$
 (20 hrs)

- 6.4 : Zeros and Poles- classification of isolated singular points, removable singularity, pole, essential singularity, order of zeros and poles
- 6.5 : Residues and Residue Theorem residue, method of evaluation of residue at poles, (Cauchy's) Residue Theorem, illustrations
- 6.6: Some Consequences of Residue theorem -
- 6.6.1: Evaluation of Real Trigonometric Integrals

- 1. James Ward Brown, Ruel Vance Churchill: Complex variables and applications (8/e), McGraw-Hill Higher Education, (2009) ISBN: 0073051942
- 2. Alan Jeffrey: Complex Analysis and Applications (2/e), Chapman and Hall/CRC Taylor Francis Group (2006), ISBN:978-1-58488-553-5
- 3. Saminathan Ponnusamy, Herb Silverman: Complex Variables with Applications Birkhauser Boston(2006) ISBN:0-8176-4457-4
- 4. John H. Mathews & Russell W. Howell: Complex Analysis for Mathematics and Engineering (6/e)
- 5. H A Priestly: Introduction to Complex Analysis (2/e), Oxford University Press, (2003), ISBN: 0-19-852562-1
- Jerrold E Marsden, Michael J Hoffman: Basic Complex Analysis (3/e) W.H Freeman, N.Y. (1999) ISBN:0-7167-2877-X

SEMESTER - V

MTS 5B28: REAL ANALYSIS - 1

4 Hours/Week

4 Credits 100 Marks[Int: 20 + Ext: 80]

Aims, Objectives and Outcomes

In this course, basic ideas and methods of real analysis are taught. Real analysis is a theoretical version of single variable calculus. So many familiar concepts of calculus are reintroduced but at a much deeper and more rigorous level than in a calculus course. At the same time there are concepts and results that are new and not studied in the calculus course but very much needed in more advanced courses. The aim is to provide students with a level of mathematical sophistication that will prepare them for further work in mathematical analysis and other fields of knowledge, and also to develop their ability to analyse and prove statements of mathematics using logical arguments. The course will enable the students

- to learn and deduce rigorously many properties of real number system by assuming a few fundamental facts about it as axioms. In particular they will learn to prove Archimedean property, density theorem, existence of a positive square root for positive numbers and so on and the learning will help them to appreciate the beauty of logical arguments and embolden them to apply it in similar and unknown problems.
- to know about sequences, their limits, several basic and important theorems involving sequences and their applications. For example, they will learn how monotone convergence theorem can be used in establishing the divergence of the harmonic series, how it helps in the calculation of square root of positive numbers and how it establishes the existence of the transcendental number e (Euler constant).
- to understand some basic topological properties of real number system such as the concept of open and closed sets, their properties, their characterization and so on.
- to state the definition of continuous functions, formulate sequential criteria for continuity and prove or disprove continuity of functions using this criteria.
- to understand several deep and fundamental results of continuous functions on intervals such as boundedness theorem, maximum minimum theorem, intermediate value theorem, preservation of interval theorem and so on.
- to realise the difference between continuity and uniform continuity and equivalence of these ideas for functions on closed and bounded interval.
- to understand the significance of uniform continuity in continuous extension theorem.

Text | Introduction to Real Analysis(4/e) : Robert G Bartle, Donald R Sherbert, John Wiley & Sons (2011) ISBN : 978-0-471-43331-6

Module - I (16 hrs)

- 1.3 : Finite and Infinite Sets definition, countable sets, denumerability of \mathbb{Q} , union of countable sets, Cantor's theorem
- 2.1 : The Algebraic and Order Properties of \mathbb{R} algebraic properties, basic results, rational and irrational numbers, irrationality of $\sqrt{2}$, Order properties, arithmetic-geometric inequality, Bernoulli's Inequality
- 2.2 : Absolute Value and the Real Line definition, basic results, Triangle Inequality, The real line, ϵ -neighborhood
- 2.3: The Completeness Property of $\mathbb R$ Suprema and Infima, alternate formulations for the supremum, The Completeness Property

Module - II (16 hrs)

- 2.4 : Applications of the Supremum Property The Archimedean Property, various consequences, Existence of $\sqrt{2}$, Density of Rational Numbers in \mathbb{R} The Density Theorem, density of irrationals
- 2.5 : Intervals definition, Characterization of Intervals, Nested Intervals, Nested Intervals Property, The Uncountability of \mathbb{R} [binary, decimal and periodic representations omitted] Cantor's Second Proof.
- 3.1 : Sequences and Their Limits definitions, convergent and divergent sequences, Tails of Sequences, Examples
- 3.2 : Limit Theorems sum, difference, product and quotients of sequences, Squeeze Theorem, ratio test for convergence
- 3.3 : Monotone Sequences definition, monotone convergence theorem, divergence of harmonic series, calculation of square root, Euler's number

Module - III (16 hrs)

3.3 : Monotone Sequences - definition, monotone convergence theorem, divergence of harmonic series, calculation of square root, Euler's number

- 3.4 : Subsequences and the Bolzano Weierstrass Theorem definition, limit of subsequences, divergence criteria using subsequence, The Existence of Monotone Subsequences, monotone subsequence theorem, The Bolzano-Weierstrass Theorem, Limit Superior and Limit Inferior
- 3.5 : The Cauchy Criterion Cauchy sequence, Cauchy Convergence Criterion, applications, contractive sequence
- 3.6 : Properly divergent sequences definition, examples, properly divergent monotone sequences, "comparison theorem", "limit comparison theorem"

Module - IV (16 hrs)

- 5.1 : Continuous Functions definition, sequential criteria for continuity, discontinuity criteria, examples of continuous and discontinuous functions, Dirichlet and Thomae function
- 5.3 : Continuous Functions on Intervals Boundedness Theorem, The Maximum Minimum Theorem, Location of Roots Theorem, Bolzano's Intermediate Value Theorem, Preservation of Intervals Theorem
- 5.4: Uniform Continuity definition, illustration, Nonuniform Continuity Criteria, Uniform Continuity Theorem, Lipschitz Functions, Uniform Continuity of Lipschitz Functions, converse, The Continuous Extension Theorem, Approximation by step functions & piecewise linear functions, Weierstrass Approximation Theorem (only statement)

- 1. Charles G. Denlinger: Elements of Real Analysis Jones and Bartlett Publishers Sudbury, Massachusetts (2011), ISBN:0-7637-7947-4 [Indian edition: ISBN- 9380853157]
- 2. David Alexander Brannan: A First Course in Mathematical Analysis Cambridge University Press, US (2006) ISBN: 9780521684248
- 3. John M. Howie: Real Analysis Springer Science & Business Media (2012) [Springer Undergraduate Mathematics Series] ISBN: 1447103416
- 4. James S. Howland: Basic Real Analysis Jones and Bartlett Publishers Sudbury, Massachusetts (2010) ISBN:0-7637-7318-2

SEMESTER - VI

MTS 6B29: LINEAR ALGEBRA

5 Hours/Week

4 Credits 100 Marks[Int: 20 + Ext: 80]

Aims, Objectives and Outcomes

An introductory treatment of linear algebra with an aim to present the fundamentals in the clearest possible way is intended here. Linear algebra is the study of linear systems of equations, vector spaces, and linear transformations. Virtually every area of mathematics relies on or extends the tools of linear algebra. Solving systems of linear equations is a basic tool of many mathematical procedures used for solving problems in science and engineering. A number of methods for solving a system of linear equations are discussed. In this process, the student will become competent to perform matrix algebra and also to calculate the inverse and determinant of a matrix. Another advantage is that the student will come to understand the modern view of a matrix as a linear transformation. The discussion necessitates the introduction of central topic of linear algebra namely the concept of a vector space. The familiarity of the students with planar vectors and their algebraic properties under vector addition and scalar multiplication will make them realize that the idea of a general vector space is in fact an abstraction of what they already know. Several examples and general properties of vector spaces are studied. The idea of a subspace, spanning vectors, basis and dimension are discussed and fundamental results in these areas are explored. This enables the student to understand the relationship among the solutions of a given system of linear equations and some important subspaces associated with the coefficient matrix of the system.

After this, some basic matrix transformations in the vector spaces \mathbb{R}^2 and \mathbb{R}^3 , having interest in the field of computer graphics, engineering and physics are studied by specially pinpointing to their geometric effect.

Just like choosing an appropriate coordinate system greatly simplifies a problem at our hand as we usually see in analytic geometry and calculus, a right choice of the basis of the vector space \mathbb{R}^n greatly simplifies the analysis of a matrix operator on it. With this aim in mind, a study on eigenvalues and eigenvectors of a given matrix (equivalently, that of the corresponding matrix operator) is taken up. Practical method of finding out the eigenvalues from the characteristic equation and the corresponding eigenvectors are also discussed. A bonus point achieved during this process is a test for the invertibility of a square matrix. As diagonal matrices are the matrices with simplest structure, the idea of diagonalization of a matrix (and hence the diagonalization of a matrix operator) is introduced and students learn a few fundamental results involving diagonalization and eigenvalues which enable them to check whether diagonalization is possible. They realise that there are matrices that cannot be diagonalized and even learn to check it. Also they are taught a well defined procedure for diagonalizing

a given matrix, if this is actually the case. The topic is progressed further to obtain the ultimate goal of spectral decomposition of a symmetric matrix. In this process, students realise that every symmetric matrix is diagonalizable and that this diagonalization can be done in a special way ie., by choosing an orthogonal matrix to perform the diagonalization. This is known as orthogonal diagonalization. Students also learn that only symmetric matrices with real entries can be orthogonally diagonalized and using Gram-Schmidt process a well defined procedure for writing such a diagonalization is also taught. In short, the course gives the students an opportunity to learn the fundamentals of linear algebra by capturing the ideas geometrically, by justifying them algebraically and by preparing them to apply it in several different fields such as data communication, computer graphics, modelling etc.

Syllabus

Text | Elementary Linear Algebra: Application Version (11/e) : Howard Anton & Chris Rorres, Wiley (2014), ISBN : 978-1-118-43441-3

Module - I (20 hrs)

Systems of Linear Equations & Matrices

- 1.1: Introduction to Systems of Linear Equations linear equation in n variables, linear system of m equations in n variables, solution, Linear Systems in Two and Three Unknowns, solution by geometric analysis, consistent and inconsistent systems, linear system with no, one, and infinite number of solutions, augmented matrix and elementary row operations
- 1.2: Gaussian elimination Considerations in Solving Linear Systems, Echelon Forms, reduced row echelon form, Elimination Methods, Gauss Jordan elimination, Gaussian elimination, Homogeneous Linear Systems, Free Variables, Free Variable Theorem for Homogeneous Systems, Gaussian Elimination and Back Substitution, Some Facts about Echelon Forms
- 1.3: Matrices and Matrix operations Matrix Notation and Terminology, row vector, column vector, square matrix of order n, Operations on Matrices, Partitioned Matrices, Matrix Multiplication by Columns and by Rows, Matrix Products as Linear Combinations, linear combination of column vectors, Column Row Expansion, Matrix Form of a Linear System, Transpose of a Matrix, Trace of a Matrix
- 1.4: Inverses and algebraic properties of matrices Properties of Matrix Addition and Scalar Multiplication, Properties of Matrix Multiplication, Zero Matrices and Properties, Identity Matrices, Inverse of a Matrix, Properties of Inverses, Solution of a Linear System by Matrix Inversion, Powers of a Matrix, Matrix Polynomials, Properties of the Transpose

- 1.5: Elementary matrices and a method for finding A^{-1} row equivalence, elementary matrix, Row Operations by Matrix Multiplication, invertibility of elementary matrices, invertibility and equivalent statements, A Method for Inverting Matrices, Inversion Algorithm, illustrations.
- 1.6: More on linear systems and invertible matrices Number of Solutions of a Linear System, Solving Linear Systems by Matrix Inversion, Linear Systems with a Common Coefficient Matrix, Properties of Invertible Matrices, equivalent statements for unique solution of Ax = b, determining consistency
- 1.7: Diagonal, Triangular and Symmetric matrices Diagonal Matrices, Inverses and Powers of Diagonal Matrices, Triangular Matrices. Properties of Triangular Matrices, Symmetric Matrices, algebraic properties of symmetric matrices, Invertibility of Symmetric Matrices
- 1.8 : Matrix transformation definition, Properties of Matrix Transformations, standard matrix, A Procedure for Finding Standard Matrices
- 2.1: Determinants by cofactor expansion minors, cofactors, cofactor expansion, Definition of a General Determinant, A Useful Technique for Evaluating 2×2 and 3×3 Determinants
- 2.2 : Evaluating determinants by row reduction a few basic theorems, elementary row operations and determinant, determinant of elementary matrices, determinant by row reduction

Module - II (20 hrs)

General Vector Spaces

- 4.1 : Real vector space Vector Space Axioms, examples, Some Properties of Vectors
- 4.2 : Subspaces definition, criteria for a subset to be a subspace, examples, Building Subspaces, linear combination, spanning, Solution Spaces of Homogeneous Systems as subspace, The Linear Transformation View point, kernel, different set of vectors spanning the subspace.
- 4.3 : Linear Independence Linear Independence and Dependence, illustrations, A Geometric Interpretation of Linear Independence, Wronskian, linear independence using wronskian
- 4.4 : Coordinates and basis Coordinate Systems in Linear Algebra, Basis for a Vector Space, finite and infinite dimensional vector spaces, illustrations, Coordinates Relative to a Basis, Uniqueness of Basis Representation
- 4.5 : Dimension Number of Vectors in a Basis, dimension, Some Fundamental Theorems, dimension of subspaces
- 4.6: Change of basis Coordinate Maps, Change of Basis, Transition Matrices, Invertibility of Transition Matrices, An Efficient Method for Computing Transition Matrices for \mathbb{R}^n , Transition to the Standard Basis for \mathbb{R}^n

Module - III (20 hrs)

4.7: Row space, Column space and Null space - vector spaces associated with matrices, consistency of linear system, Bases for Row Spaces, Column Spaces, and Null Spaces, basis from row echelon form, Basis for the Column Space of a Matrix, row equivalent matrices and relationship between basis for column space, Bases Formed from Row and Column Vectors of a Matrix

- 4.8: Rank Nullity and Fundamental matrix spaces equality of dimensions of row and column spaces, Rank and Nullity, Dimension Theorem for Matrices, The Fundamental Spaces of a Matrix, rank of a matrix and its transpose, A Geometric Link Between the Fundamental Spaces, orthogonal complement, invertibility and equivalent statements, Applications of Rank, Over determined and Under determined Systems
- 4.9: Basic matrix transformations in \mathbb{R}^2 and \mathbb{R}^3 Reflection Operators, Projection Operators, Rotation Operators, Rotations in \mathbb{R}^3 , Dilations and Contractions, Expansions and Compressions, Shears, Orthogonal Projections onto Lines Through the Origin, Reflections About Lines Through the Origin
- 4.10: Properties of matrix transformation- Compositions of Matrix Transformations, One to One Matrix Transformations, Kernel and Range, fundamental relationship between invertibility of a matrix and its matrix transformation, Inverse of a One-to-One Matrix Operator
- 4.11: Geometry of matrix operators- Transformations of Regions, Images of Lines Under Matrix Operators, Geometry of Invertible Matrix Operators, Elementary matrix and its matrix transformation, consequence

$$\mathrm{Module-IV}$$
 (20 hrs)

- 5.1: Eigen values and Eigen Vectors definition, Computing Eigenvalues and Eigenvectors, characteristic equation, alternative ways of describing eigen values, Finding Eigenvectors and Bases for Eigenspaces, Eigenvalues and Invertibility, Eigenvalues of General Linear Transformations,
- 5.2: Diagonalization The Matrix Diagonalization Problem, linear independence of eigen vectors and diagonalizability, Procedure for Diagonalizing a Matrix, Eigenvalues of Powers of a Matrix, Computing Powers of a Matrix, Geometric and Algebraic Multiplicity
- 6.1: Inner Product definition of General inner product, Euclidean inner product (or the standard inner product) on \mathbb{R}^n , norm of a vector, properties (upto and including theorem 6.1.1), a few examples (only example 7 and example 10) [rest of the section omitted]
- 6.2: Angle and orthogonality in Inner product spaces only the definition of orthogonality in a real inner product space (to be motivated by the relation in the definition (3) of section 3.2) and

examples(2),(3) and (4)

- 6.3: Gram–Schmidt Process definition of Orthogonal and Orthonormal Sets, examples, linear independence of orthogonal set, orthonormal basis, Coordinates Relative to Orthonormal Bases [Orthogonal Projections omitted] The Gram–Schmidt Process [only statement of Theorem 6.3.5 and the step by step construction technique are required; derivation omitted], illustrations examples 8 and 9, Extending Orthonormal Sets to Orthonormal Bases [rest of the section omitted]
- 7.1: Orthogonal Matrices definition, characterisation of orthogonal matrices, properties of orthogonal matrices, Orthogonal Matrices as Linear Operators, a geometric interpretation [rest of the section omitted]
- 7.2 : Orthogonal Diagonalization The Orthogonal Diagonalization Problem, Conditions for Orthogonal Diagonalizability, Properties of Symmetric Matrices, Procedure for Orthogonally Diagonalizing an $n \times n$ Symmetric Matrix, Spectral Decomposition (upto and including example 2) [rest of the section omitted]

- Jim DeFranza, Daniel Gagliardi: Introduction to Linear Algebra with Applications Waveland Press, Inc (2015), ISBN: 1-4786-2777-8
- 2. Otto Bretscher: Linear Algebra with Applications (5/e) Pearson Education, Inc (2013), ISBN: 0-321-79697-7
- 3. Ron Larson, Edwards, David C Falvo: Elementary Linear Algebra (6/e), Houghton Mifflin Harcourt Publishing Company (2009) ISBN: 0-618-78376-8
- 4. David C. Lay, Steven R. Lay, Judi J. McDonald: Linear Algebra and its Application (5/e) Pearson Education, Inc(2016) ISBN: 0-321-98238-X
- Martin Anthony, Michele Harvey: Linear Algebra: Concepts and Methods Cambridge University Press (2012) ISBN: 978-0-521-27948-2
- 5. Jeffrey Holt: Linear Algebra with Applications W. H. Freeman and Company (2013), ISBN: 0-7167-8667-2

SEMESTER - VI

MTS 6B30 : REAL ANALYSIS - 2

4 Hours/Week

 $3 \text{ Credits} \quad 75 \text{ Marks}[\text{Int: } 15 + \text{Ext: } 60]$

Aims, Objectives and Outcomes

The course is built upon the foundation laid in Basic Analysis course of fifth semester. The course thoroughly exposes one to the rigour and methods of an analysis course. One has to understand definitions and theorems of text and study examples well to acquire skills in various problem solving techniques. The course will teach one how to combine different definitions, theorems and techniques to solve problems one has never seen before. One shall acquire ability to realise when and how to apply a particular theorem and how to avoid common errors and pitfalls. The course will prepare students to formulate and present the ideas of mathematics and to communicate them elegantly.

- Develop the notion of Riemann integrability of a function using the idea of tagged partitions and calculate the integral value of some simple functions using the definition.
- Understand a few basic and fundamental results of integration theory.
- Formulate Cauchy criteria for integrability and a few applications of it. In particular they learn to use Cauchy criteria in proving the non integrability of certain functions.
- Understand classes of functions that are always integrable
- Understand two forms of fundamental theorem of calculus and their significance in the practical problem of evaluation of an integral.
- Find a justification for 'change of variable formula' used in the practical problem of evaluation of an integral.
- Prove convergence and divergence of sequences of functions and series
- Understand the difference between pointwise and uniform convergence of sequences and series of functions
- Answer a few questions related to interchange of limits.
- Learn and find out examples/counter examples to prove or disprove the validity of several mathematical statements that arise naturally in the process/context of learning.
- Understand the notion of improper integrals, their convergence, principal value and evaluation.
- Learn the properties of and relationship among two important improper integrals namely beta and gamma functions that frequently appear in mathematics, statistics, science and engineering.

Text (1)	Introduction to Real Analysis(4/e) : Robert G Bartle, Donald R Sherbert, John Wiley
	& Sons (2011), ISBN: 978-0-471-43331-6
Text (2)	Improper Riemann Integrals: Ioannis M. Roussos CRC Press by Taylor & Francis
	Group, LLC(2014), ISBN: 9781466588080 (eBook PDF)
Text (3)	Elementary Differential Equations and Boundary Value Problems (11/e): William E
	Boyce, Richard C Diprima And Douglas B Meade John Wiley & Sons(2017) ISBN:
	1119169879

Module - I Text (1) (16 hrs)

- 7.1 : Riemann Integral Partitions and Tagged Partitions, Riemann sum, Riemann integrability, examples, Some Properties of the Integral, Boundedness Theorem
- 7.2: Riemann Integrable Functions Cauchy Criterion, illustrations, The Squeeze Theorem, Classes of Riemann Integrable Functions, integrability of continuous and monotone functions, The Additivity Theorem
- 7.3: The Fundamental Theorem The Fundamental Theorem (First Form), The Fundamental Theorem (Second Form), Substitution Theorem, Lebesgue's integrability Criterion, Composition Theorem, The Product Theorem, Integration by Parts, Taylor's Theorem with the Remainder

Module - II Text (1) (16 hrs)

- 8.1 : Pointwise and Uniform Convergence definition, illustrations, The Uniform Norm, Cauchy Criterion for Uniform Convergence
- 8.2: Interchange of Limits examples leading to the idea, Interchange of Limit and Continuity, Interchange of Limit and Derivative [only statement of theorem 8.2.3 required; proof omitted] Interchange of Limit and Integral, Bounded convergence theorem(statement only) [8.2.6 Dini's theorem omitted]
- 9.4 : Series of Functions (A quick review of series of real numbers of section 3.7 without proof) definition, sequence of partial sum, convergence, absolute and uniform convergence, Tests for Uniform Convergence, Weierstrass M Test (only upto and including 9.4.6)

Module – III Text (2) (16 hrs)

- 1.1: Definitions and Examples
- 1.2 : Cauchy Principal Value
- 1.3 : Some Criteria of Existence
- 2.1 : Calculus Techniques ['2.1.1 Applications' Omitted]

- 2.2: Integrals Dependent on Parameters upto and including example 2.2.4
- 2.6: The Real Gamma and Beta Functions upto and including Example 2.6.18

Module - IV Text (3) (16 hrs)

- 10.1 : Two Point Boundary Value Problems
- 10.2 : Fourier Series
- 10.3: The Fourier Convergence Theorem
- 10.4: Even and Odd Functions
- 10.5 : Separation of Variables; Heat Conduction in a Rod
- 10.7: The Wave Equation: Vibrations of an Elastic String

- Charles G. Denlinger: Elements of Real Analysis Jones and Bartlett Publishers Sudbury, Massachusetts (2011), ISBN:0-7637-7947-4 [Indian edition: ISBN- 9380853157]
- 2. David Alexander Brannan: A First Course in Mathematical Analysis Cambridge University Press, US (2006) ISBN: 9780521684248
- 3. John M. Howie: Real Analysis Springer Science & Business Media (2012) [Springer Undergraduate Mathematics Series] ISBN: 1447103416
- 4. James S. Howland: Basic Real Analysis Jones and Bartlett Publishers Sudbury, Massachusetts (2010) ISBN:0-7637-7318-2
- 5. Terence Tao: Analysis I & II (3/e), TRIM 37 & 38, Springer Science + Business Media Singapore 2016; Hindustan book agency(2015), ISBN: 9789811017896 (eBook) & ISBN: 978-981101804(eBook)
- Richard R Goldberg: Methods of Real Analysis Oxford and IBH Publishing Co.Pvt.Ltd. New Delhi (1970)
- Saminathan Ponnusamy: Foundations of Mathematical Analysis Birkhauser (2012), ISBN: 978-0817682910
- 8. William F Trench: Introduction to Real Analysis, ISBN: 0130457868
- 9. Ajith Kumar & S Kumaresan : A Basic Course in Real Analysis CRC Press, Taylor & Francis Group (2014), ISBN: 9781482216387 (eBook PDF)
- 10. Hugo D Junghenn: A Course in Real Analysis CRC Press, Taylor & Francis Group(2015), ISBN: 9781482219289 (eBook PDF)

ELECTIVE COURSES

SEMESTER - VI (Elective Course)

MTS 6B31(E01): NUMERICAL ANALYSIS

3 Hours/Week

3 Credits 75 Marks[Int: 15 + Ext: 60]

Aims, Objectives and Outcomes

The goal of numerical analysis is to provide techniques and algorithms to find approximate numerical solution to problems in several areas of mathematics where it is impossible or hard to find the actual/closed form solution by analytical methods and also to make an error analysis to ascertain the accuracy of the approximate solution. The subject addresses a variety of questions ranging from the approximation of functions and integrals to the approximate solution of algebraic, transcendental, differential and integral equations, with particular emphasis on the stability, accuracy, efficiency and reliability of numerical algorithms. The course enables the students to

- Understand several methods such as bisection method, fixed point iteration method, regula falsi
 method etc. to find out the approximate numerical solutions of algebraic and transcendental
 equations with desired accuracy.
- Understand the concept of interpolation and also learn some well known interpolation techniques.
- Understand a few techniques for numerical differentiation and integration and also realize their merits and demerits.

Syllabus

Text

Numerical Analysis (10/e): Richard L. Burden, J Douglas Faires, Annette M. Burden, Brooks Cole Cengage Learning (2016) ISBN:978-1-305-25366-7

Module - I (16 hrs)

Solutions of Equations in One Variable

Note: Students should be familiar with concepts and definitions such as 'round off error', 'rate of convergence'etc. discussed in sections 1.2 and 1.3

Introduction

2.1: The Bisection Method

- 2.2: Fixed Point Iteration
- 2.3: Newton's Method and its Extensions Newton's Method (Newton Raphson method), Convergence using Newton's Method, The Secant Method, The Method of False Position
- 2.4 : Error Analysis for Iterative Methods Order of Convergence, linear and quadratic convergence, Multiple Roots, Modified Newton's method for faster convergence

[Algorithms are omitted]

Module - II (16 hrs)

Interpolation and Polynomial Approximation

Introduction

- 3.1 : Interpolation and the Lagrange Polynomial motivation, Lagrange Interpolating Polynomials, error bound
- 3.2 : Data Approximation and Neville's Method motivation, Neville's Method, recursive method to generate Lagrange polynomial approximations.
- 3.3: Divided Differences $k^{\rm th}$ divided difference, Newton's divided difference formula, Forward Differences, Newton Forward-Difference Formula, Backward Differences, Newton Backward-Difference Formula, Centered Differences, Stirling's formula. [Algorithms are omitted]

Module - III (16 hrs)

Numerical Differentiation and Integration

Introduction

- 4.1: Numerical Differentiation approximation of first derivative by forward difference formula, backward difference formula, Three Point Formulas, Three Point Endpoint Formula, Three Point Midpoint Formula [Five Point Formulas, Five Point Endpoint Formula, Five Point Midpoint Formula omitted] Second Derivative Midpoint Formula to approximate second derivative, Round Off Error Instability
- 4.3 : Elements of Numerical Integration numerical quadrature, The Trapezoidal Rule, Simpson's Rule, Measuring Precision, Closed Newton Cotes Formulas, Simpson's Three Eighth's rule, Open Newton-Cotes Formulas
- 4.4 : Composite Numerical Integration composite Simpson's rule, composite trapezoidal rule, composite midpoint rule, round off error stability
- 4.7 : Gaussian Quadrature motivation, Legendre Polynomial, Gaussian Quadrature on Arbitrary Intervals

[Algorithms are omitted]

- 1. Kendall E. Atkinson, Weimin Han: Elementary Numerical Analysis (3/e), John Wiley & Sons(2004) ISBN:0-471-43337-3[Indian Edition by Wiley India, ISBN: 978-81-265-0802-0]
- 2. James F. Epperson: An Introduction to Numerical Methods and Analysis (2/e) John Wiley & Sons (2013), ISBN: 978-1-118-36759-9
- 3. Timothy Sauer: Numerical Analysis (2/e), Pearson (2012), ISBN: 0-321-78367-0
- 4. S S Sastri: Introductory Methods of Numerical Analysis (5/e), PHI Learning Pvt. Ltd. (2012), ISBN:978-81-203-4592-8
- 5. Ward Cheney, David Kincaid: Numerical Mathematics and Computing (6/e), Thomson Brooks/Cole (2008), ISBN: 495-11475-8

SEMESTER - VI (Elective Course)

MTS 6B31(E02): INTRODUCTION TO GEOMETRY

3 Hours/Week

3 Credits 75 Marks[Int: 15 + Ext: 60]

Aims, Objectives and Outcomes

Geometry is, basically, the study concerned with questions of shape, size, and relative position of planar and spatial objects. The classical Greek geometry, also known as Euclidean geometry after the work of Euclid, was once regarded as one of the highest points of rational thought, contributing to the thinking skills of logic, deductive reasoning and skills in problem solving.

In the early 17 th century, the works of Rene Descartes and Pierre de Fermat put the foundation stones for the creation of analytic geometry where the idea of a coordinate system was introduced to simplify the treatment of geometry and to solve a wide variety of geometric problems.

Desargues, a contemporary of Descartes was fascinated towards the efforts of artists/painters to give a realistic view of their art works/paintings usually done on a flat surface such as canvas or paper. To get a realistic view of a three dimensional object/scene depicted on a flat surface, a right impression of height, width, depth and position in relation to each other of the objects in the scene is required. This idea is called perspective in art. If two artists make perspective drawings of the same object, their drawings shall not be identical but there shall be certain properties of these drawings that remain the same or that remain invariant. The study of such invariant things crystallised into what is now called projective geometry. Now days, it plays a major role in computer graphics and in the design of camera models.

Another development is the evolution of affine geometry. In simple terms, if we look at the shadows of a rectangular window on the floor under sunlight, we could see the shadows not in perfect rectangular form but often in the shape of a parallelogram. The size of shadows also changes with respect to the position of the sun. Hence, neither length nor angle is invariant in the transformation process. However, the opposite sides of the images are always parallel. So this transformation keeps parallelism intact. The investigation of invariants of all shadows is the basic problem of affine geometry.

Towards the end of nineteenth century, there were several different geometries: Euclidean, affine, projective, inversive, spherical, hyperbolic, and elliptic to name a few. It was the idea of Felix Klein to bring the study of all these different geometries into a single platform. He viewed each geometry as a space together with a group of transformations of that space and regarded those properties of figures left unaltered by the group as geometrical properties. In this course, it is intended to take up a study of a few geometries based on the philosophy of Klein.

Upon successful completion of the course, students will be able to

- 1. Understand several basic facts about parabola, hyperbola and ellipse (conics) such as their equation in standard form, focal length properties, and reflection properties, their tangents and normal.
- 2. Recognise and classify conics.
- 3. Understand Kleinian view of Euclidean geometry.
- 4. Understand affine transformations, the inherent group structure, the idea of parallel projections and the basic properties of parallel projections.
- 5. Understand the fundamental theorem of affine geometry, its use in the proof of Median theorem, Ceva's theorem, Menelaus' theorem etc.
- 6. Understand which conics are affine-congruent to each other
- 7. Realise the basic difference in identifying two geometric objects in Euclidean and affine geometries.
- 8. Understand Kleinian view of projective geometry
- 9. Understand the idea of homogeneous coordinate of a point in projective plane and write down the equation of a line in projective plane passing through two homogeneous coordinate
- 10. Know collinearity property and incidence property in projective plane.
- 11. Check whether a transformation is indeed projective and also to find the composite and inverse of projective transformations.
- 12. Identify some projective properties
- 13. Write down the projective transformation that maps a given set of four points to another set of four points.
- 14. Appreciate the advantage of interpreting a Euclidean theorem as a projective theorem by learning a simpler proof for Desargues and Pappu's theorem.
- 15. Understand the concept of cross ratio and calculate it
- 16. Find an application of cross ratio in the context of aerial photography.

Text | Geometry (2/e) : David A Brannan, Mathew F Espen, Jeremy J Gray, Cambridge University | Press (2012), ISBN : 978-1-107-64783-1

Module - I (16 hrs)

Conics

- 1.1.1: Conic Sections
- 1.1.3 : Focus Directrix Definition of the Non-Degenerate Conics definition, parabola in standard form, ellipse in standard form, hyperbola in standard form, Rectangular Hyperbola, Polar Equation of a Conic
- 1.1.4 : Focal Distance Properties of Ellipse and Hyperbola Sum of Focal Distances of Ellipse, Difference of Focal Distances of Hyperbola,
- 1.2: Properties of Conics Tangents, equation of tangents to ellipse, hyperbola, and parabola, polar of a point w.r.t. unit circle, normal, Reflections, The Reflection Law, Reflection Property of the Ellipse, Reflection Property of the Hyperbola, Reflection Property of the Parabola, Conics as envelopes of tangent families
- 1.3 : Recognizing Conics equation of conic in general form, identifying a conic

Module - II (16 hrs)

Affine Geometry

- 2.1 : Geometry and Transformations What is Euclidean Geometry? Isometry, Euclidean properties, Euclidean transformation, Euclidean-Congruence
- 2.2 : Affine Transformations and Parallel Projections- Affine Transformations, Basic Properties of Affine Transformations, Parallel Projections, Basic Properties of Parallel Projections, Affine Geometry, Midpoint Theorem, Conjugate Diameters Theorem, Affine Transformations and Parallel Projections, affine transformations as composite of two parallel projections
- 2.3: Properties of Affine Transformations-Images of Sets Under Affine Transformations, The Fundamental Theorem of Affine Geometry, Proofs of the Basic Properties of Affine Transformations
- 2.4 : Using the Fundamental Theorem of Affine Geometry-The Median Theorem, Ceva's Theorem, converse, Menelaus' Theorem, converse [subsection "2.4.4. Barycentric Coordinates" omitted]
- 2.5 : Affine Transformations and Conics-Classifying Non-Degenerate Conics in Affine Geometry, A few affine properties, Applying Affine Geometry to Conics

Module - III (16 hrs)

Projective Geometry: Lines

- 3.1: Perspective Perspective in Art, Mathematical Perspective, Desargues' Theorem
- 3.2: The Projective Plane \mathbb{RP}^2 -Projective Points, Projective Lines, Embedding Planes, An equivalent definition of Projective Geometry
- 3.3: Projective Transformations The Group of Projective Transformations, Some Properties of Projective Transformations, Fundamental Theorem of Projective Geometry, [The subsection "3.3.4.Geometrical Interpretation of Projective Transformations" omitted]
- 3.4: Using the Fundamental Theorem of Projective Geometry Desargues' Theorem and Pappus' Theorem, [The subsection "3.4.2. Duality "omitted]
- 3.5 : Cross-Ratio-Another Projective Property, properties of cross ratio, Unique Fourth Point Theorem, Pappus' Theorem, Cross-Ratio on Embedding Planes, An Application of Cross-Ratio

- 1. George A Jennings: Modern Geometry with Applications University text, Springer (1994), ISBN:0-387-94222-X
- 2. Walter Meyer: Geometry and its Application(2/e) Elsever, Academic Press (2006)ISBN:0-12-369427-0
- 3. Judith N Cederberg: A Course in Modern Geometries(2/e) UTM, Springer (2001) ISBN: 978-1-4419-3193-1
- 4. Patric J Ryan: Euclidean and Non Euclidean Geometry-An Analytic Approach Cambridge University Press, International Student Edition (2009) ISBN:978-0-521- 12707-3
- 5. David C Kay: College Geometry: A Unified Approach CRC Press Tayloe and Francic Group (2011) ISBN: 978-1-4398-1912-8 (Ebook-PDF)
- 6. James R Smart: Modern Geometries(5/e) Brooks/Cole Publishing Co.,(1998) ISBN:0- 534-35188-3
- 7. Michele Audin: Geometry University text, Springer(2003) ISBN:3-540-43498-48

SEMESTER - VI (Elective Course)

MTS 6B31(E03): LINEAR PROGRAMMING

3 Hours/Week

3 Credits 75 Marks[Int: 15 + Ext: 60]

Aims, Objectives and Outcomes

Linear programming problems are having wide applications in mathematics, statistics, computer science, economics, and in many social and managerial sciences. For mathematicians it is a sort of mathematical modelling process, for statisticians and economists it is useful for planning many economic activities such as transport of raw materials and finished products from one place to another with minimum cost and for military heads it is useful for scheduling the training activities and deployment of army personnel. The emphasis of this course is on nurturing the linear programming skills of students via. the algorithmic solution of small-scale problems, both in the general sense and in the specific applications where these problems naturally occur. On successful completion of this course, the students will be able to

- 1. solve linear programming problems geometrically
- 2. understand the drawbacks of geometric methods
- 3. solve LP problems more effectively using Simplex algorithm via. the use of condensed tableau of A.W. Tucker
- 4. convert certain related problems, not directly solvable by simplex method, into a form that can be attacked by simplex method.
- 5. understand duality theory, a theory that establishes relationships between linear programming problems of maximization and minimization
- 6. understand game theory
- 7. solve transportation and assignment problems by algorithms that take advantage of the simpler nature of these problems

Text

Linear Programming and Its Applications : James K. Strayer Undergraduate Texts in Mathematics Springer (1989), ISBN: 978-1-4612-6982-3

Module - I (16 hrs)

Chapter 1 Geometric Linear Programming:

Profit Maximization and Cost Minimization, typical motivating examples, mathematical formulation, Canonical Forms for Linear Programming Problems, objective functions, constraint set, feasible solution, optimal solution, Polyhedral Convex Sets, convex set, extreme point, theorems asserting existence of optimal solutions, The Two Examples Revisited, graphical solutions to the problems, A Geometric Method for Linear Programming, the difficulty in the method, Concluding Remarks

Chapter 2 The Simplex Algorithm: -

Canonical Slack Forms for Linear Programming Problems; Tucker Tableaus, slack variables, Tucker tableaus, independent variables or non basic variables, dependent variables or basic variables. An Example: Profit Maximization, method of solving a typical canonical maximization problem, The Pivot Transformation, The Pivot Transformation for Maximum and Minimum Tableaus, An Example: Cost Minimization, method of solving a typical canonical minimization problem, The Simplex Algorithm for Maximum Basic Feasible Tableaus, The Simplex Algorithm for Maximum Tableaus, Negative Transposition; The Simplex Algorithm for Minimum Tableaus, Cycling, Simplex Algorithm Anti cycling Rules, Concluding Remarks

Module - II (16 hrs)

Chapter 3 Noncanonical Linear Programming Problems : -

Unconstrained Variables, Equations of Constraint, Concluding Remarks

Chapter 4 : Duality Theory : -

Duality in Canonical Tableaus, The Dual Simplex Algorithm, The Dual Simplex Algorithm for Minimum Tableaus, The Dual Simplex Algorithm for Maximum Tableaus, Matrix Formulation of Canonical Tableaus, The Duality Equation, Duality in Noncanonical Tableaus, Concluding Remarks

Module - III (16 hrs)

Chapter 5 Matrix Games:-

An Example; Two-Person Zero-Sum Matrix Games, Domination in a Matrix Game, Linear Programming Formulation of Matrix Games, The Von Neumann Minimax Theorem, The Example Revisited, Two More Examples, Concluding Remarks

Chapter 6 Transportation and Assignment Problems:-

The Balanced Transportation Problem, The Vogel Advanced-Start Method (VAM), The Transportation Algorithm, Another Example, Unbalanced Transportation Problems, The Assignment Problem, The Hungarian Algorithm, Concluding Remarks, The Minimum-Entry Method, The Northwest-Corner Method

- 1. Robert J. Vanderbei: Linear Programming: Foundations and Extensions (2/e), Springer Science+Business Media LLC (2001), ISBN: 978-1-4757-5664-7
- 2. Frederick S Hiller, Gerald J Lieberman: Introduction to Operation Research (10/e), McGraw-Hill Education, 2 Penn Plaza, New York (2015), ISBN: 978-0-07-352345-3
- 3. Paul R. Thie, G. E. Keough: An Introduction to Linear Programming and Game Theory (3/e), John Wiley and Sons, Ins. (2008), ISBN: 978-0-470-23286-6
- Louis Brickman: Mathematical Introduction to Linear Programming and Game Theory UTM, Springer Verlag, NY (1989), ISBN :0-387-96931-4
- 5. Jiri Matoušek, Bernd Gartner: Understanding and Using Linear Programming Universitext, Springer-Verlag Berlin Heidelberg (2007), ISBN: 978-3-540-30697-9